

Power calculations in SAS

PROC Power

PROC GLMPower

PROC Mixed

Simulations (Data Step)



Syntax (a peek at things to come)

1)The Power and Sample Size Application

2)

```
PROC POWER< just print options>;  
LOGISTIC<options>;  
MULTREG<options>;  
ONECORR<options>;  
ONESAMPLEFREQ<options>;  
ONESAMPLEMEANS<options>;  
ONEWAYANOVA <options>;  
PAIREDFREQ<options>;  
PAIREDMEANS<options>;  
TWO SAMPLEFREQ<options>;  
TWO SAMPLEMEANS<options>;  
TWO SAMPLESURVIVAL<options>;  
TWO SAMPLEWILCOXON<options>;  
  
PLOT<plot-options> </ graph-options>;  
Run;
```

3) First, you create the exemplary data set to specify means and weights;

Data Exemplary;

Input datalines;

input Pressure \$ Fluid \$ Y_bar CellWt;

datalines;

High Water 36.9 4

High EZD1 35.0 2

Low Water 34.3 6

Low EZD1 32.4 3 ; Run;

**PROC GLMPower data=exemplary
options > ;**

BY variables ;

CLASS variables ;

**CONTRAST 'label' effect values
< . . . effect values > < / options > ;**

MODEL dependents = independents ;

PLOT < plot-options >< / graph-options > ;

POWER < options > ;

Run;

4)Simulations

How to save typing when asking for multiple analysis

Keyword-Lists: Keywords separated by spaces e.g. **SIDES = 2 U**

Number-Lists: Can be TWO things

1) Valued: **NTOTAL = 30 50 70 100**

or **NTOTAL = 30 to 70 by 20 100**

or 2) Missing **NTOTAL = .**

Grouped-Number-Lists:

Values for each group are “crossed” with the values from the other group

GROUPNS = 20 25 | 30 40 50

→ **(20,30)(20,40)(20,50) (25,30)(25,40)(25,50)**

Options for plotting

PLOT <plot-options> </ graph-options>

INTERPOL=JOIN | NONE

KEY=BYCURVE <(bycurve-options)>

KEY=BYFEATURE <(byfeature-options)>

KEY=ONCURVES

NUMBERS=OFF | ON

POS=BOTTOM | INSET

POS=BOTTOM | INSET

POS= INSET

MARKERS=ANALYSIS | COMPUTED | NICE | NONE

MAX=number | DATAMAX

MIN=number | DATAMIN

NPOINTS=number

NPTS=number

STEP=number

VARY (feature <BY parameter-list> <, ..., feature <BY parameter-list>>)

X=EFFECT | N | POWER

XOPTS=(x-options)

CROSSREF=NO | YES

REF=number-list

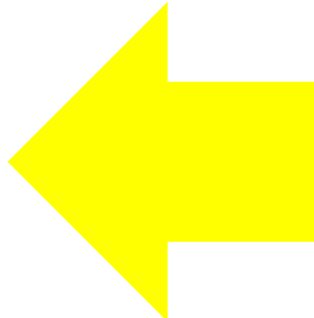
Y=EFFECT | N | POWER

YOPTS=(y-options)

CROSSREF=NO | YES

REF=number-list

DESCRIPTION='string '



The plot option alone has over twenty options and, inside SAS Power Procs, is not unusual in that characteristic

Options for plotting

Plot <plot-options> </ graph-options>

PROC POWER;

PAIREDMEANS MeanDiff= .2 .4 .6 Stddev=1

Corr= .3 .7

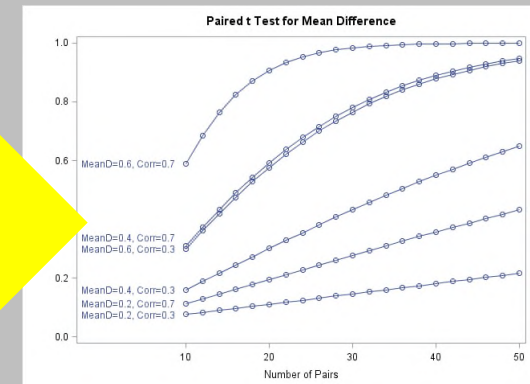
Alpha=.05 Npairs=25 Power=.;

PLOT X=N Min=10 Max=50 Key=OnCurves;

RUN;

Y is Power
X is N

Yu can plot Power, N or Effect Size
and you can control Y and X axis



PROC POWER;

PAIREDMEANS MeanDiff= .2 .4 .6 Stddev=1

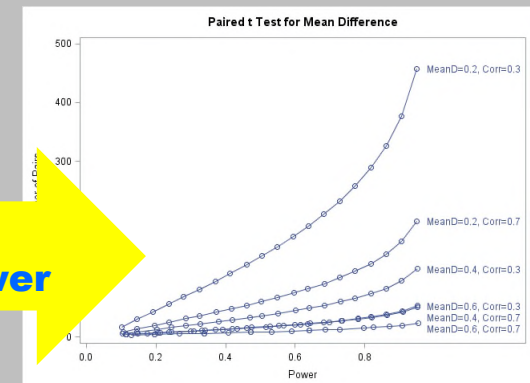
Corr= .3 .7

Alpha=.05 Npairs=. Power=.9;

PLOT X=power Min=.1 Max=.95 Key=OnCurves;

RUN;

Y is N
X is Power



☹ NOT explored at all ☹
Y=EFFECT | N | POWER

PROC POWER;

PAIREDMEANS MeanDiff= .2 .4 .6 Stddev=1

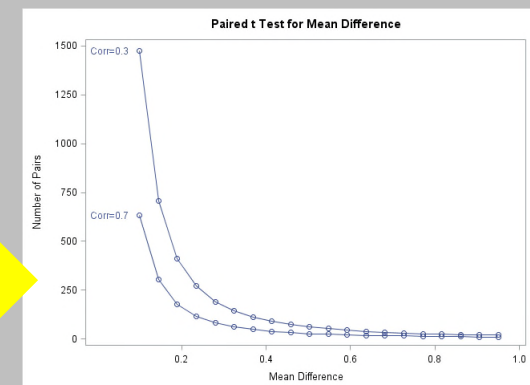
Corr= .3 .7

Alpha=.05 Npairs=. Power=.9;

PLOT X=EFFECT Min=.1 Max=.95

Key=OnCurves; RUN;

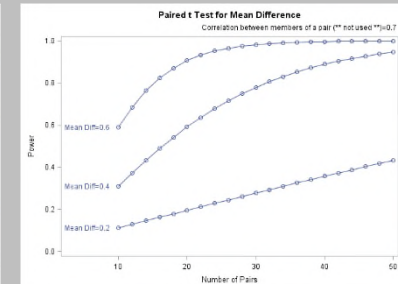
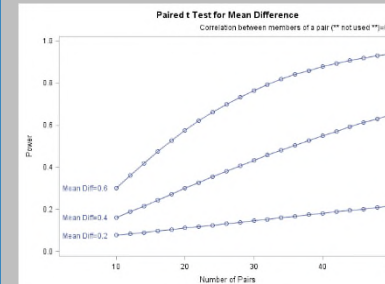
Y is N
X Mean Difference



Options for plotting

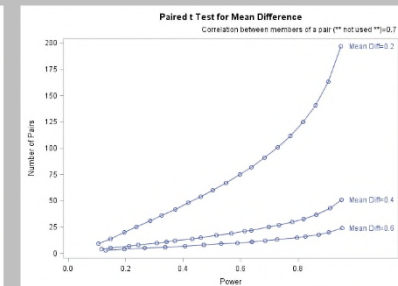
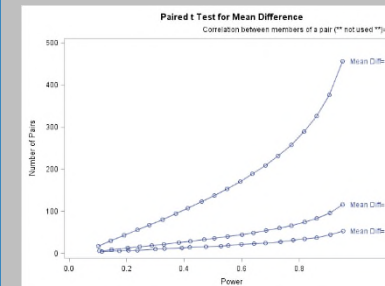
PLOT <plot-options> </ graph-options>

```
PROC POWER;
PAIREDMEANS MeanDiff= .2 .4 .6 Stddev=1
Corr= .3 .7
Alpha=.05 Npairs=25 Power=.;
PLOT X=N Min=10 Max=50 Key=OnCurves;
VarY(Panel BY Corr); RUN;
```



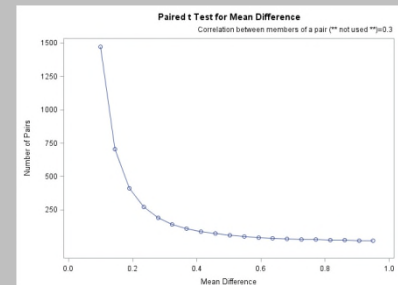
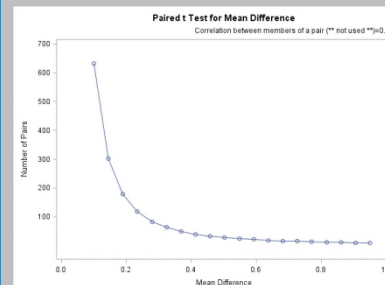
Y is Power X is N

```
PROC POWER;
PAIREDMEANS MeanDiff= .2 .4 .6 Stddev=1
Corr= .3 .7
Alpha=.05 Npairs=. Power=.9;
PLOT X=power Min= .1 Max= .95
Key=OnCurves VarY(Panel BY Corr); RUN;
```



Y is N X is Power

```
PROC POWER;
PAIREDMEANS MeanDiff= .2 .4 .6 Stddev=1
Corr= .3 .7
Alpha=.05 Npairs=. Power=.9;
PLOT X=EFFECT Min=.1 Max=.95
Key=OnCurves VarY(Panel BY Corr); RUN;
```



Y is N X Mean Difference

Proc Power:

Code from SAS Documentation

PROC Power

LOGISTIC Statement

MULTREG Statement

ONECORR Statement

ONESAMPLEFREQ Statement

ONESAMPLEMEANS Statement

ONEWAYANOVA Statement

PAIREDFREQ Statement

PAIREDMEANS Statement

TWOSAMPLEFREQ Statement

TWOSAMPLEMEANS Statement

TWOSAMPLESURVIVAL Statement

TWOSAMPLEWILCOXON Statement

LOGISTIC Statement Options

TEST= Specifies the statistical analysis

ALPHA= Specifies the significance level

COVARIATES= distrib. of predictor variables

TESTPREDICTOR= distrib. of predictor var. being tested

VARDIST= Distribution for predictor var.

Specify effects

CORR= multiple corr. between the predictor & covariates

COVODDSRATIOS= odds ratios for the covariates

COVREGCOEFFS= regression coeff. for the covariates

DEFAULTUNIT= Default change in the predictor variables

INTERCEPT= Specifies the intercept

RESPONSEPROB= Specifies response prob.

TESTODDSRATIO= Specifies the odds ratio being tested

TESTREGCOEFF= Regress. Coeff. 4 predictor variable

UNITS= Specifies the changes in the predictor variables

NFRACTIONAL allows fractional input/output for N

NTOTAL= Specifies the sample size

POWER= Specifies the desired power

DEFAULTNBINS= default # of categories 4 each X var.

NBINS= Specifies the # of categories for predictor vars

OUTPUTORDER= output order of paramaters

LOGISTIC: power and N calculations for a likelihood ratio chi-square test allowing for 1

Show results

proc power;

logistic

vardist("x1a") = normal(0, 2)

vardist("x1b") = normal(0, 3)

vardist("x2") = poisson(7)

vardist("x3a") =

ordinal((-5 0 5) : (.3 .4 .3))

vardist("x3b") =

ordinal((-5 0 5) : (.4 .3 .3))

testpredictor = "x1a" "x1b"

covariates = "x2" | "x3a" "x3b"

responseprob = 0.15

testoddsratio = 1.75

covoddsratios = (2.1 1.4)

ntotal = 100 ;

power = .;

plot x=n min=100 max=200;

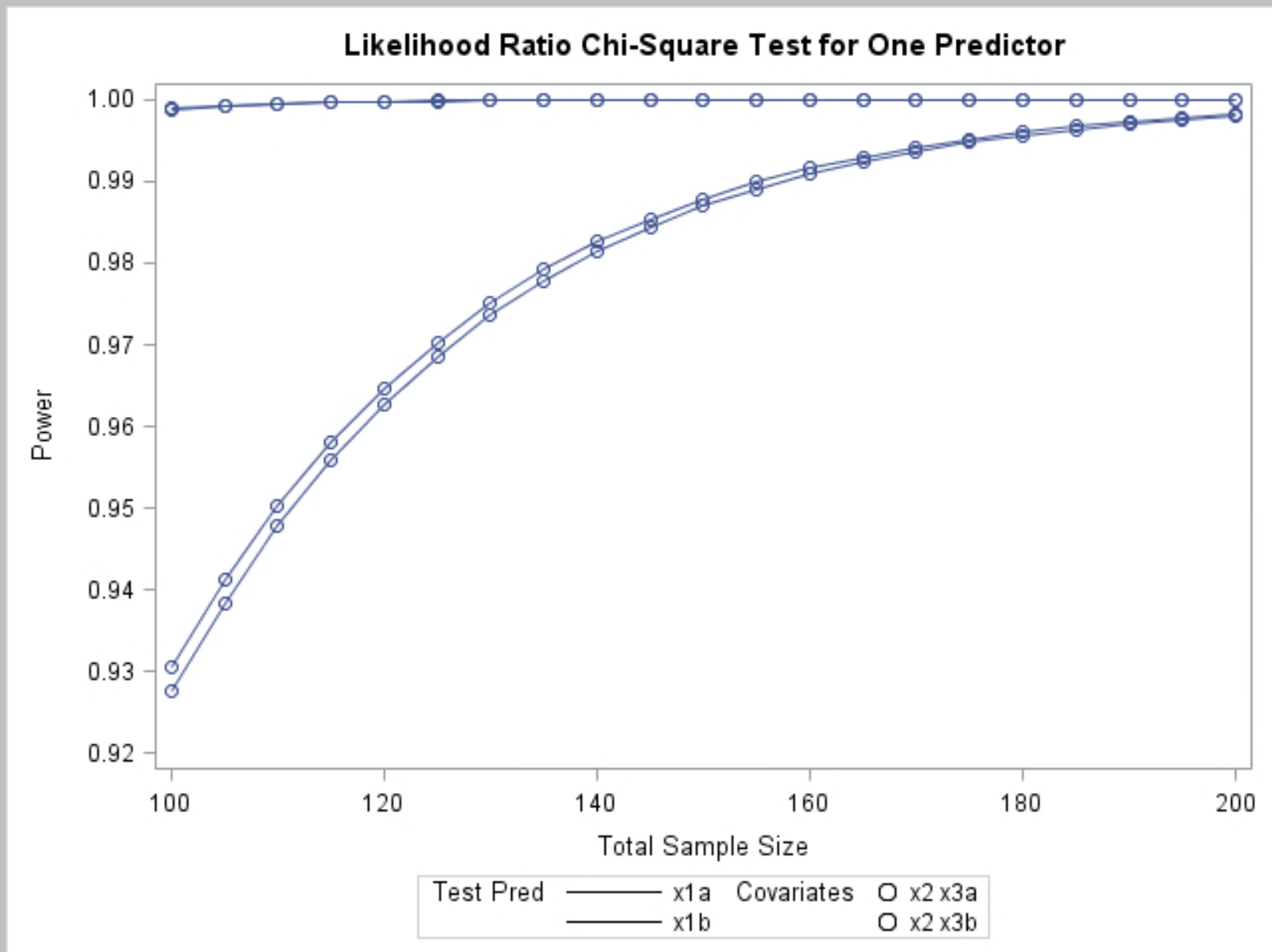
run;

Fixed Scenario Elements

| | |
|-------------------------------|-----------------------------|
| Method | Shieh-O'Brien approximation |
| Response Probability | 0.15 |
| Odds Ratio for Test Predictor | 1.75 |
| Covariate Odds Ratios | 2.1 1.4 |
| Total Sample Size | 100 |
| Alpha | 0.05 |

Computed Power

| Index | Test Pred | Covariates | | Test Pred Unit | Cov Units | | Total N Bins | Power |
|-------|-----------|------------|-----|----------------|-----------|---|--------------|-------|
| 1 | x1a | x2 | x3a | 1 | 1 | 1 | 300 | 0.931 |
| 2 | x1a | x2 | x3b | 1 | 1 | 1 | 300 | 0.927 |
| 3 | x1b | x2 | x3a | 1 | 1 | 1 | 300 | 0.999 |
| 4 | x1b | x2 | x3b | 1 | 1 | 1 | 300 | 0.999 |



```
proc power; Multreg  
model = random  
nfullpredictors = 7  
ntestpredictors = 3  
partialcorr = 0.35  
ntotal = 100  
power = .; run;
```

**Model = FIXED for
categorical predictors,
Model = RANDOM for MVN
continuous predictors**

**You can also express effects in terms of
R2:**

```
proc power; Multreg  
model = fixed  
nfullpredictors = 7  
ntestpredictors = 3  
rsquarefull = 0.9  
rsquarediff = 0.1  
ntotal = .  
power = 0.9; run;
```

Show Fixed results

Example of Multreg PROC Power Syntax

* Options within MULTREG for PROC POWER:

Model = FIXED for categorical predictors,
Model = RANDOM for MVN continuous predictors

Alpha = .05 is default, choose others as you wish

INCLUDE ONLY TWO OF THREE BELOW for **N** predictors:

NFullPredictors = # of predictors total in regression

NReducedPredictors = # of predictors in reduced alternative model

NTestPredictors = difference in # of predictors between models

SPECIFYING EFFECT SIZE: INCLUDE ONLY TWO OF THREE BELOW RSQ OPTIONS

RsqFull = one or more R² values of full model

RsqReduced = one or more R² values of reduced model

RsqDiff = one or more diff in R² between full and reduced models

OR CHOOSE PartialCorr = one or more partial correlations to be detected

NTotal = Total sample size (put . if you want it to be calculated)

Power = . if you want power to be calculated */

Restrictions on Option Combinations

To specify X use any **two** of these three options:

1 of 3) # of X in the full model
(**NFULLPREDICTORS**=)

2 of 3) # of X in the reduced model
(**NREDUCEDPREDICTORS**=)

3 of 3) # of X being tested
(**NTESTPREDICTORS**=)

Restrictions on Option Combinations

To specify the effect, choose one of the following parameterizations:

1 of 2) partial correlation (by using the **PARTIALCORR**= option)

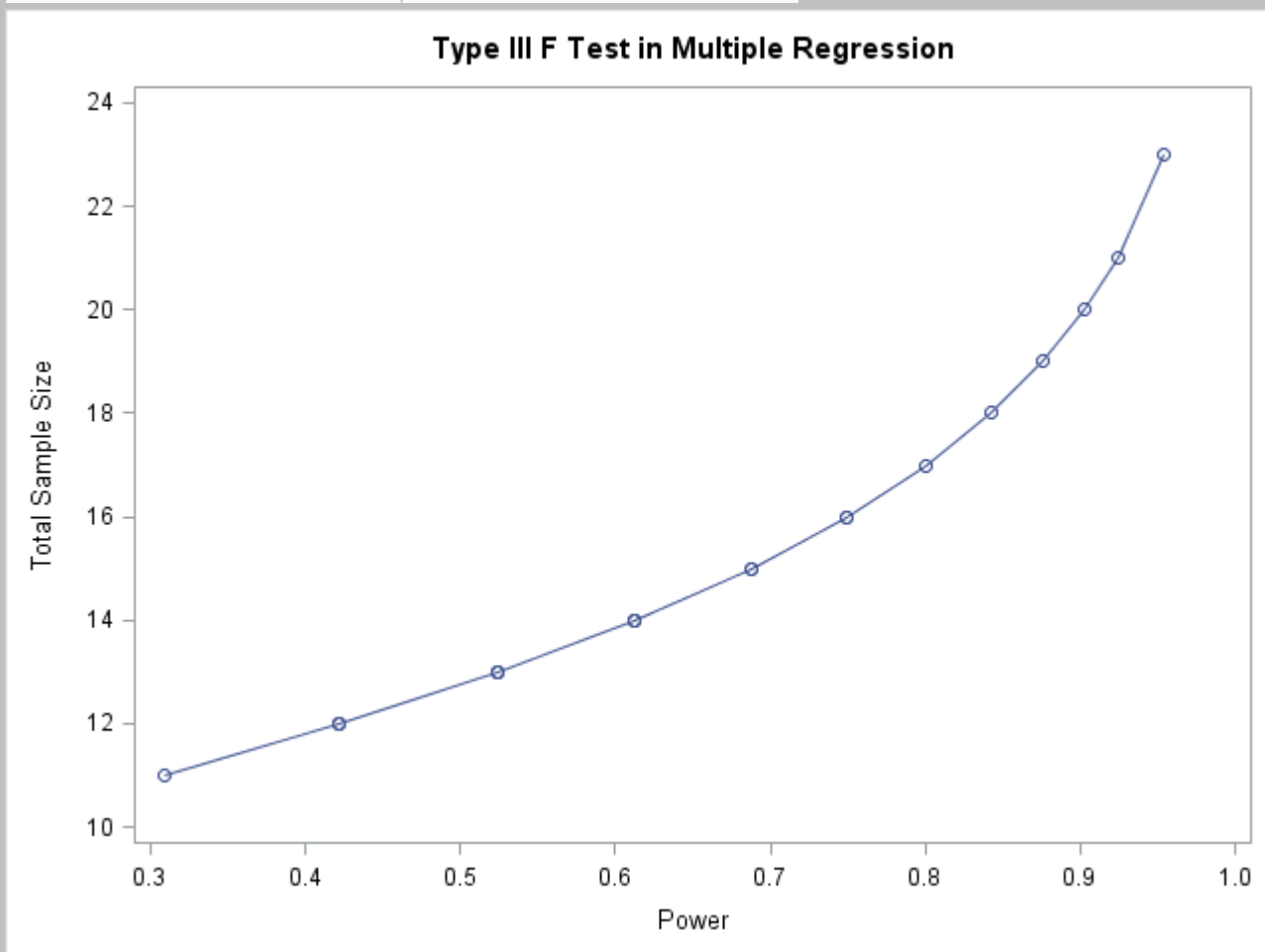
2 of 2) R² for the full and reduced models (by using any **two** of)

RSQUAREDIFF= ,
RSQUAREFULL= , and
RSQUAREREDUCED=)



| Fixed Scenario Elements | |
|------------------------------------|---------|
| Method | Exact |
| Model | Fixed X |
| Number of Predictors in Full Model | 7 |
| Number of Test Predictors | 3 |
| R-square of Full Model | 0.9 |
| Difference in R-square | 0.1 |
| Nominal Power | 0.9 |
| Alpha | 0.05 |

| Computed N Total | |
|------------------|---------|
| Actual Power | N Total |
| 0.903 | 20 |



Power Analysis for General Linear Models in SAS (Multreg)

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

```
PROC POWER;  
MULTREG  
Model =random  
NFullPredictors = 4  
NTestPredictors = 1  
Alpha = .05  
PartialCorr = .1 .2 .3 .4 .5  
NTotal = 100  
Power = . ;  
PLOT X = N Min=50 Max=200  
Key =OnCurves;  
RUN;
```

NFullPredictors = # of predictors total in regression

NReducedPredictors = # of predictors in reduced alternative model

NTestPredictors = difference in # of predictors between models

Show results

Plot Power, N or effect size and you can control Y and X axis

Power Analysis for General Linear Models in SAS (Multreg)

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The POWER Procedure
Type III F Test in Multiple Regression

Fixed Scenario Elements

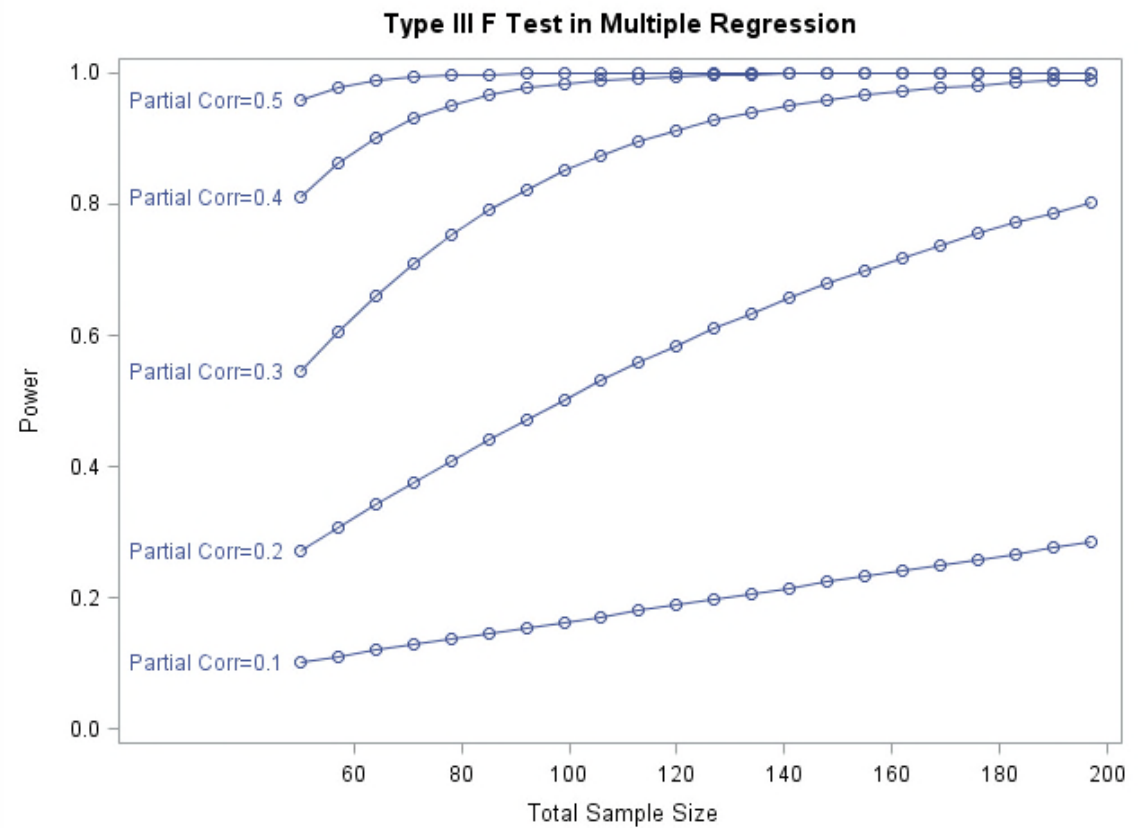
| | |
|-------------------------------|----------|
| Method | Exact |
| Model | Random X |
| # of Predictors in Full Model | 4 |
| # Test Predictors | 1 |
| Alpha | 0.05 |
| Total Sample Size | 100 |

Computed Power

| Index | Partial Corr | Power |
|-------|--------------|-------|
| 1 | 0.1 | 0.164 |
| 2 | 0.2 | 0.506 |
| 3 | 0.3 | 0.855 |
| 4 | 0.4 | 0.985 |
| 5 | 0.5 | >.999 |

Power to Detect Range of Partial Correlations

Will calculate power for sample sizes around Ntotal



Power Analysis for General Linear Models in SAS (Multreg)

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

Show results

```
TITLE1 "Power to Detect Range of Incremental R2";
TITLE2 "Will calculate power for sample sizes around
Ntotal";
PROC POWER;
MULTREG
Model=random
NFullPredictors = 3
NTestPredictors = 3
Alpha = .05
RsqrReduced = 0
RsqrDiff = .05 .10 .15 .20
NTotal = 100
Power = .;
PLOT X = N Min = 50 Max = 200
Key =OnCurves;
RUN;
```

NFullPredictors = # of predictors total in regression

NReducedPredictors = # of predictors in reduced alternative model

NTestPredictors = difference in # of predictors between models

RsqrFull = one or more R2 values of full model

RsqrReduced = one or more R2 values of reduced model

RsqrDiff = one or more diff in R2 between full and reduced models

Plot Power, N or effect size and you can control Y and X axis

Power Analysis for General Linear Models in SAS (Multreg)

The POWER Procedure
Type III F Test in Multiple Regression

Fixed Scenario Elements

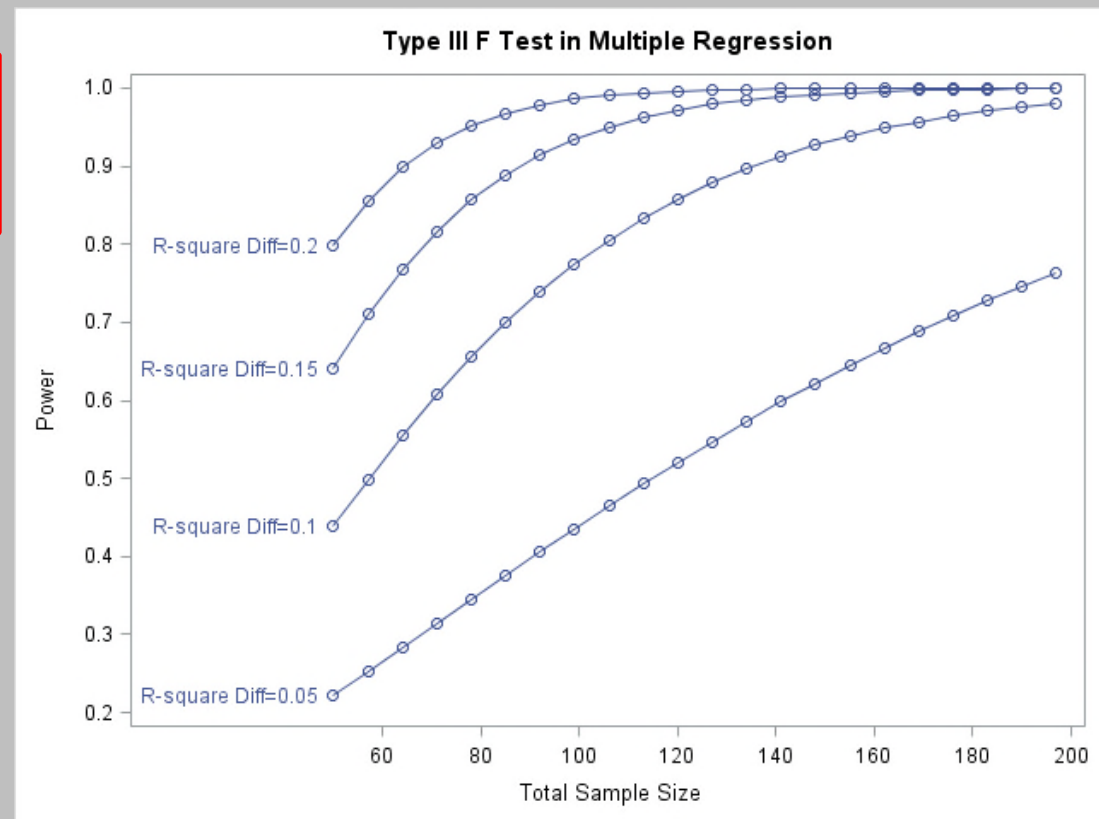
| | |
|-------------------------------|----------|
| Method | Exact |
| Model | Random X |
| # of Predictors in Full Model | 3 |
| # of Test Predictors | 3 |
| Alpha | 0.05 |
| R-square of Reduced Model | 0 |
| Total Sample Size | 100 |

Computed Power

| Index | R-square Diff | Power |
|-------|---------------|-------|
| 1 | 0.05 | 0.440 |
| 2 | 0.10 | 0.778 |
| 3 | 0.15 | 0.937 |
| 4 | 0.20 | 0.987 |

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf


Power to Detect Range of Incremental R²
Will calculate power for sample sizes around Ntotal



Power Analysis for General Linear Models in SAS (Multreg)

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

```
TITLE1 "Power to Detect Range of Incremental R2";  
TITLE2 "Will calculate Ntotal for 80% power at each R2";  
PROC POWER;  
MULTREG  
Model =random  
NFullPredictors = 3  
NTestPredictors = 3  
Alpha = .05  
RsqReduced = 0  
RsqDiff = .05 .10 .15 .20  
NTotal = .  
Power = .80;  
PLOT X =Effect Min = .05 Max = .30  
Key =OnCurves;  
RUN ;
```



**Show
results**



**Plot Power, N or effect size
and you can control Y and X axis**

Power Analysis for General Linear Models in SAS (Multreg)

The POWER Procedure
Type III F Test in Multiple Regression

Fixed Scenario Elements

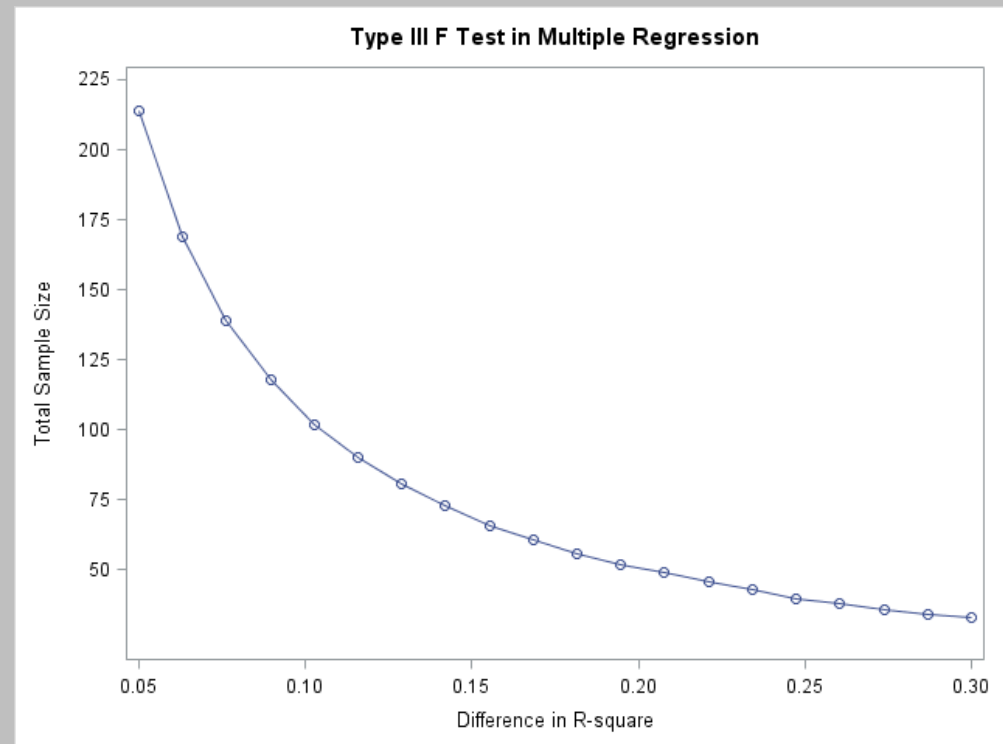
| | |
|-------------------------------|----------|
| Method | Exact |
| Model | Random X |
| # of Predictors in Full Model | 3 |
| # of Test Predictors | 3 |
| Alpha | 0.05 |
| RSQ: Reduced Model | 0 |
| Nominal Power | 0.8 |

Computed N Total

| Index | R-Sq Diff | Actual Power | N Total |
|-------|-----------|--------------|---------|
| 1 | 0.05 | 0.800 | 214 |
| 2 | 0.10 | 0.801 | 105 |
| 3 | 0.15 | 0.804 | 69 |
| 4 | 0.20 | 0.807 | 51 |

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

Power to Detect Range of Incremental R²
Will calculate Ntotal for 80% power at each R²



X is effect size:
Difference in r-square

RsqReduced = 0

RsqDiff = .05 .10 .15 .20

/*Fisher's z Test for Pearson Correlation*/

PROC Power; onecorr

dist=fisherz

nullcorr = 0.15

corr = 0.35

ntotal = 180

power = .;

run;

/*T Test for Pearson Correlation*/

PROC Power; onecorr

dist=t

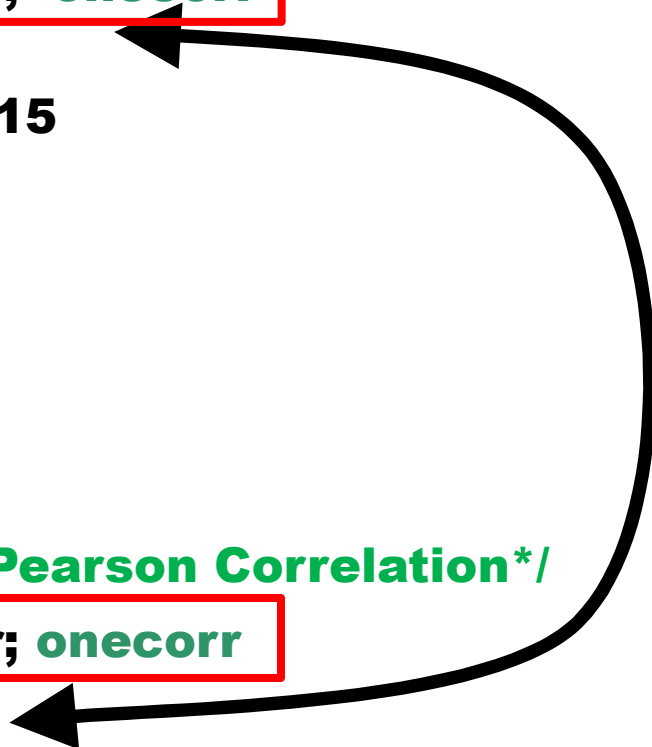
npartialvars = 4

corr = 0.45

ntotal = .

power = 0.85;

run



Example of One Corr PROC Power Syntax

ONECORR

power and N for simple and partial Pearson correlation between two variables. Supports Fisher's Z & the T test

Summary of Options

| Option | Description |
|--------|-------------|
|--------|-------------|

Define analysis

DIST= Underlying distrib. assumed for the test statistic

TEST= Specifies the statistical analysis

Specify analysis information

ALPHA= Specifies the significance level

MODEL= Assumed distribution of the variables

NPARTIALVARS= # of var. adjusted for in the correlation

NULLCORR= Specifies the null value of the correlation

SIDES= One-Two tails and direction of test

CORR= Specifies t

Specify sample size


NFRACTIONAL Allows fractional N

NTOTAL= Specifies/requests the sample size

POWER= specifies/requests the power of the test

OUTPUTORDER= Output order

```
proc power;  
onecorr  
dist=fisherz  
nullcorr = 0.15  
corr = 0.35  
ntotal = 180  
power = .;  
plot x=n min=100  
max=200;  
run;
```



Show
results

The POWER Procedure

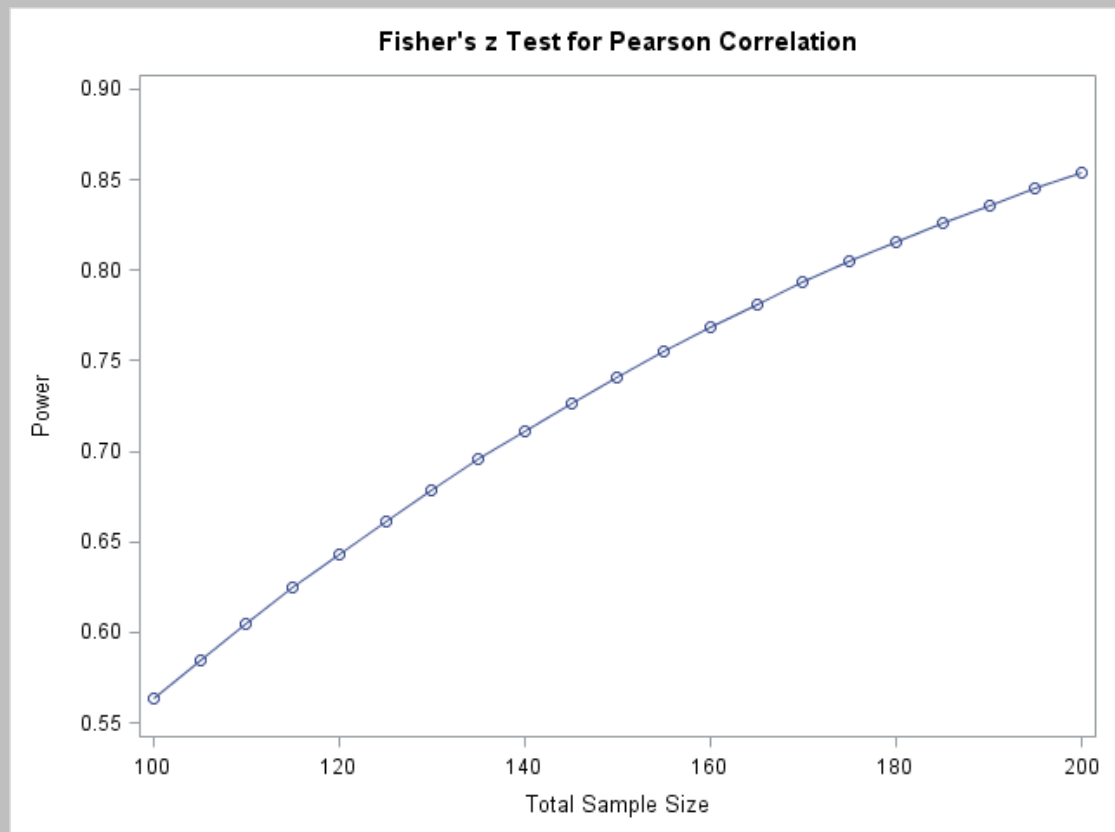
Fisher's z Test for Pearson Correlation

Fixed Scenario Elements

| | |
|------------------------------------|--------------------------------|
| Distribution | Fisher's z transformation of r |
| Method | Normal approximation |
| Null Correlation | 0.15 |
| Correlation | 0.35 |
| Total Sample Size | 180 |
| Number of Sides | 2 |
| Nominal Alpha | 0.05 |
| Number of Variables Partialled Out | 0 |

Computed Power

| Actual Alpha | Power |
|--------------|-------|
| 0.05 | 0.816 |



Exact Test of a Binomial Proportion

```
PROC Power; onesamplefreq
```

```
test=exact
```

```
nullproportion = 0.2
```

```
proportion = 0.3
```

```
ntotal = 100
```

```
power = .; run;
```

the z test of a binomial proportion.

```
PROC Power; onesamplefreq
```

```
test=z method=normal
```

```
nullproportion = 0.8
```

```
proportion = 0.85
```

```
sides = u ntotal = .
```

```
power = .9; run;
```

ztest of a binomial proportion with
a continuity adjustment.

```
PROC Power; onesamplefreq
```

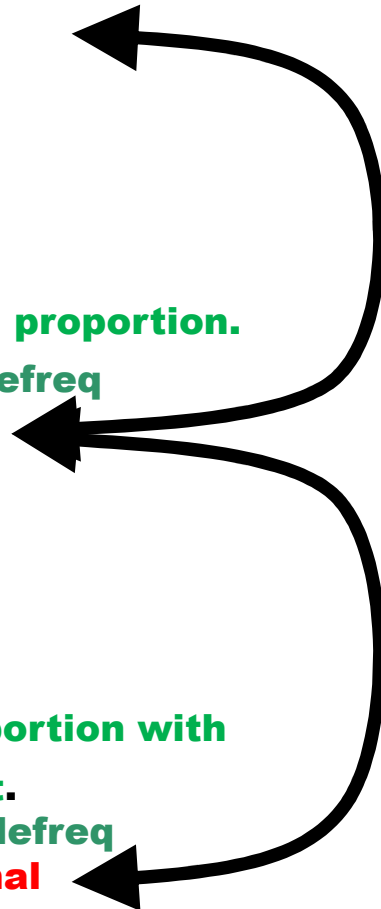
```
test=adjz method=normal
```

```
nullproportion = 0.15
```

```
proportion = 0.1
```

```
sides = l ntotal = .
```

```
power = .9; run;
```



Exact Equivalence Test for a Binomial Proportion

specify equivalence bounds by EQUIVBOUNDS=

```
proc power; OneSampleFreq
```

```
test=equiv_exact
```

```
proportion = 0.35 equivbounds = (0.2 0.4)  
ntotal = 50 power = .; run;
```

With NULLPROPORTION= and MARGIN=

```
proc power; OneSampleFreq
```

```
test=equiv_exact
```

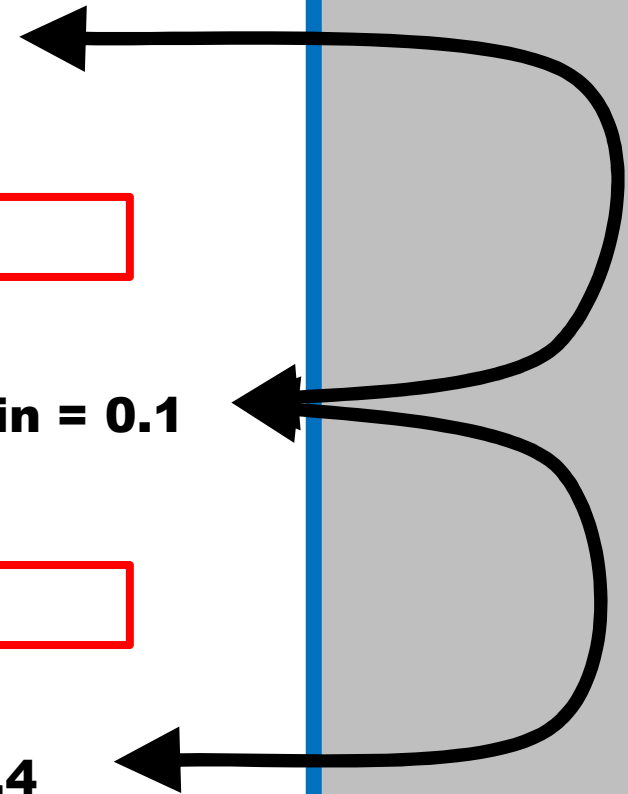
```
proportion = 0.35 nullproportion = 0.3 margin = 0.1  
ntotal = 50 power = .; run;
```

Use a combination of LOWER= and UPPER=

```
proc power; OneSampleFreq
```

```
test=equiv_exact
```

```
proportion = 0.35 lower = 0.2          upper = 0.4  
ntotal = 50 power = .; run;
```



One-Sample T Test

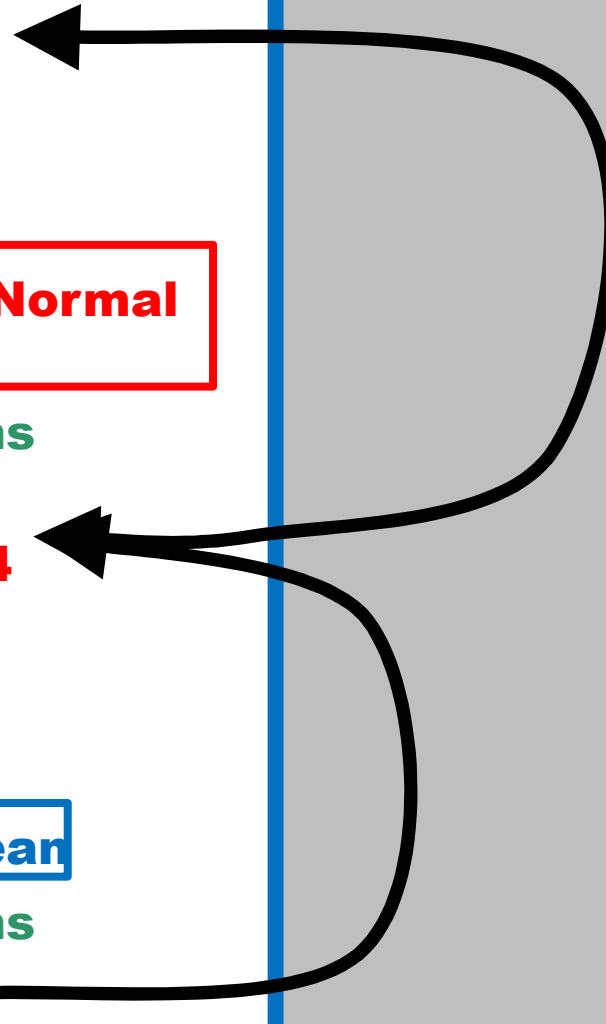
```
PROC Power; OneSampleMeans  
test=t mean = 7  
stddev = 3  
ntotal = 50 power = .; run;
```

Equivalence Test for Mean of Normal Data

```
PROC Power; OneSampleMeans  
test=equiv  
lower = 2 upper = 7 mean = 4  
stddev = 3  
ntotal = 100 power = .; run;
```

Confidence interval for the mean

```
PROC Power; OneSampleMeans  
ci = t halfwidth = 14  
stddev = 8  
ntotal = 50 probwidth = .; run;
```



Overall F Test

PROC Power; OneWayANNOVA
test=overall

groupmeans = 3 | 7 | 8
stddev = 4
npergroup = 50
power = .;
run;

Many Options in One way
ANOVA

Contrast

PROC Power;
OneWayANNOVA
test=contrast

contrast = (1 0 -1)
groupmeans = 3 | 7 | 8
stddev = 4

groupns = (20 40 40)

power = .;
run;

Balanced Contrast

PROC Power;
OneWayANNOVA
test=contrast

contrast = (1 0 -1)
groupmeans = 3 | 7 | 8
stddev = 4

npergroup = 50

power = .;
run;

Unbalanced Contrast

PROC Power;
OneWayANNOVA
test=contrast

contrast = (1 0 -1)
groupmeans = 3 | 7 | 8
stddev = 4

groupweights = (1 2 2)
ntotal = .

power = 0.9;
run;

PROC POWER;

* 3 groups: Drug, Drug+Caffeine, Placebo, using means from previous research;

* SDs should have been 10.8, 12.4, and 7.1, but it only allows a common SD;

ONEWAYANOVA

GroupMeans = 11.4 | 16.7 | 4.0

Stddev = 10.0

GroupWeights = (1 1 1) (2 2 1)

/*space between numbers not (111) (221)*/

Test =Overall

Alpha =.05

Ntotal =90

Power = .;

PLOT X = N Min = 30 Max = 180

Key = OnCurves;

RUN

;

Overall test of means
3 means
2 groupweights

No Contrasts

Show results

Power Analysis for General Linear Models in SAS (Multreg)

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The POWER Procedure
Overall F Test for One-Way ANOVA

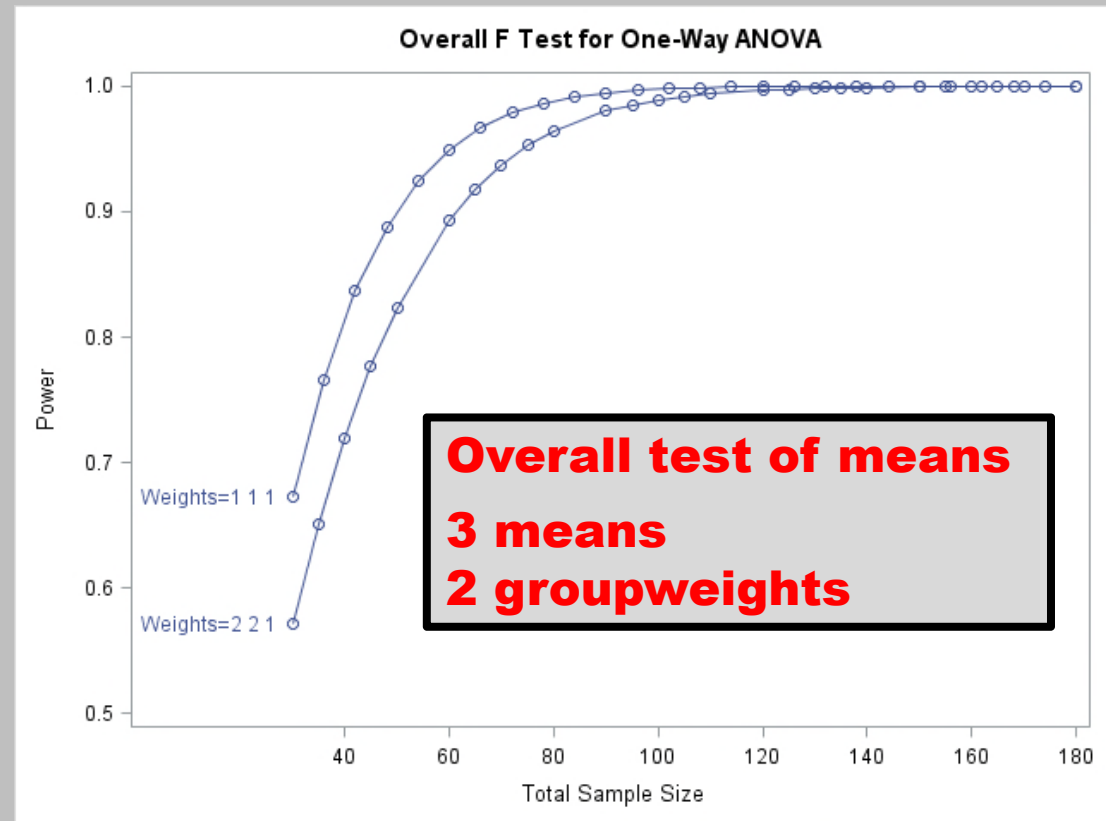
Power to Detect Range of Omnibus
Between-Group Mean Differences
Will calculate power for sample sizes
around Ntotal

Fixed Scenario Elements

| | |
|--------------------|-------------|
| Method | Exact |
| Alpha | 0.05 |
| Group Means | 11.4 16.7 4 |
| Standard Deviation | 10 |
| Total Sample Size | 90 |

Computed Power

| Index | Weights | | | Power |
|-------|---------|---|---|-------|
| 1 | 1 | 1 | 1 | 0.995 |
| 2 | 2 | 2 | 1 | 0.980 |



TITLE1 "Power to Detect Range of Specific Between-Group Mean Differences";

TITLE2 "Will calculate power for sample sizes around Ntotal";

PROC POWER;

*** 3 groups: Drug, Drug+Caffeine, Placebo, using means from previous research;**

*** SDs should have been 10.8, 12.4, and 7.1, but it only allows a common SD;**

OneWayANOVA

GroupMeans = 11.4 | 16.7 | 4.0

Stddev = 10.0

GroupWeights = (1 1 1)(2 2 1)

Test = Contrast

Alpha = .05

Ntotal = 90

Power = .

Contrast = (-1 -1 2) (-1 1 0);

PLOT X = N Min=30 Max = 180

Key = OnCurves;

RUN

;

**3 groups with
2 possible weighting plans
(possibly cost driven?)**

**Test two
Contrasts**

**Show
results**

Proc Power: OneWayAnova

The POWER Procedure Single DF Contrast in 1-Way ANOVA

Fixed Scenario Elements

| | |
|---------------------|-------------|
| Method | Exact |
| Alpha | 0.05 |
| Group Means | 11.4 16.7 4 |
| Standard Dev. | 10 |
| Total Sample Size | 90 |
| Number of Sides | 2 |
| Null Contrast Value | 0 |

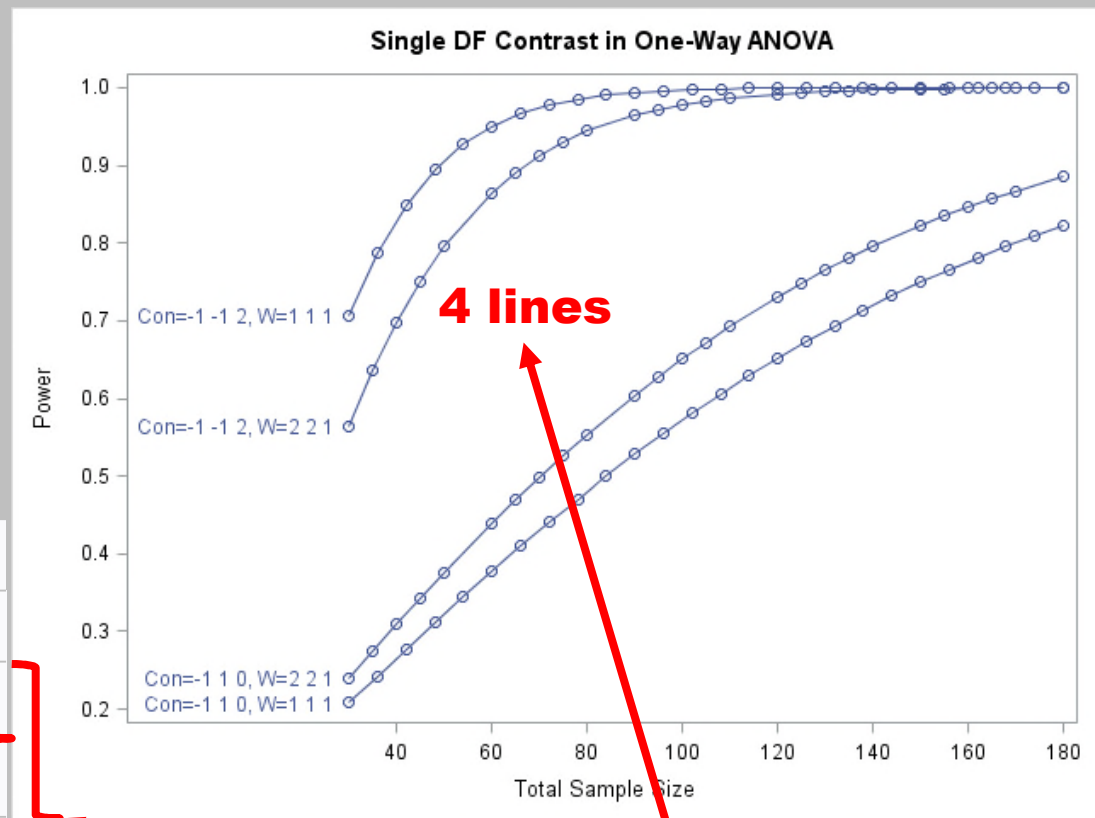
Computed Power

| Index | Contrast | | | Weights | | | Power |
|-------|----------|----|---|---------|---|---|-------|
| 1 | -1 | -1 | 2 | 1 | 1 | 1 | 0.994 |
| 2 | -1 | -1 | 2 | 2 | 2 | 1 | 0.965 |
| 3 | -1 | 1 | 0 | 1 | 1 | 1 | 0.528 |
| 4 | -1 | 1 | 0 | 2 | 2 | 1 | 0.604 |

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

Power to Detect Range of Specific
Between-Group Mean Differences

Will calculate power for sample sizes
around Ntotal



Test two Contrasts and two
weighting schemes

**Examples are from
Statistical Power
Analysis Using SAS and R
Shows Contrasts
(55 pages and many examples)**

Proc Power: OneWayAnova

Statistical Power Analysis Using SAS and R

Contrasts 55 pages and many examples

<http://digitalcommons.calpoly.edu/cgi/viewcontent.cgi?article=1002&context=statspa>

The POWER Procedure Single DF Contrast in One-Way ANOVA

```
Proc Power;  
OneWayANOVA test=contrast  
contrast = ( 1 -1 0 0 0 0 )  
           ( 0 1 0 0 -1 0 )  
           ( 0 0 1 -1 0 0 )  
groupmeans=(5 4 6 11 12 9 )  
std= 4  
npergroup= .  
power= .8;  
run ;
```

Fixed Scenario Elements

| | |
|---------------------|---------------|
| Method | Exact |
| Group Means | 5 4 6 11 12 9 |
| Standard Deviation | 4 |
| Nominal Power | 0.8 |
| Number of Sides | 2 |
| Null Contrast Value | 0 |
| Alpha | 0.05 |

**Test three Contrasts
6 means**

Computed N Per Group

| Index | Contrast | | | | | | Actual Power | N Per Group |
|-------|----------|----|---|----|----|---|--------------|-------------|
| 1 | 1 | -1 | 0 | 0 | 0 | 0 | 0.801 | 252 |
| 2 | 0 | 1 | 0 | 0 | -1 | 0 | 0.858 | 5 |
| 3 | 0 | 0 | 1 | -1 | 0 | 0 | 0.822 | 11 |

3 answers


```
TITLE1 "Power to Detect Range of Omnibus Between-Group Mean Differences";  
TITLE2 "Will calculate power for sample sizes around Ntotal";
```

```
PROC POWER;
```

```
* 3 groups: Drug, Drug+Caffeine, Placebo, using std mean differences;
```

```
OneWayANOVA
```

```
GroupMeans = .4 | .6 | 0
```

```
Stddev =1
```

```
GroupWeights =(1 1 1 )( 2 2 1)
```

```
Test = Overall
```

```
Alpha =.05
```

```
Ntotal = 90
```

```
Power = .;
```

```
PLOT X = N Min=30 Max=180
```

```
Key =OnCurves;
```

```
RUN
```

```
;
```

OneWayANOVA

3 Means =.4 .6 0.0

Two weighting schemes

Overall test of means –

No contrasts

**Show
results**

The POWER Procedure Overall F Test for One-Way ANOVA

**Power to Detect Range of Omnibus
Between-Group Mean Differences
Will calculate power for sample sizes
around Ntotal**

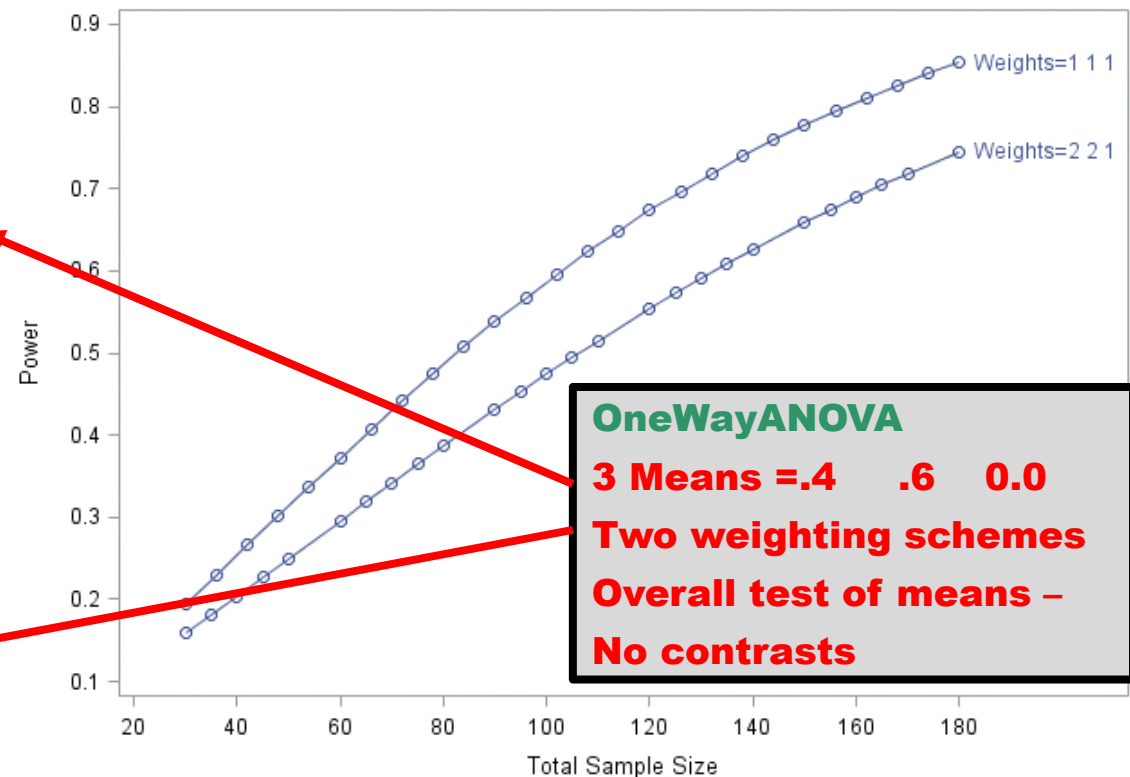
Fixed Scenario Elements

| | |
|--------------------|-----------|
| Method | Exact |
| Alpha | 0.05 |
| Group Means | 0.4 0.6 0 |
| Standard Deviation | 1 |
| Total Sample Size | 90 |

Computed Power

| Index | Weights | | | Power |
|-------|---------|---|---|-------|
| 1 | 1 | 1 | 1 | 0.538 |
| 2 | 2 | 2 | 1 | 0.431 |

Overall F Test for One-Way ANOVA



```
TITLE1 "Power to Detect Range of Specific Between-Group Mean Differences";  
TITLE2 "Will calculate power for sample sizes around Ntotal";  
PROC POWER ;  
* 3 groups: Drug, Drug+Caffeine, Placebo, using std mean differences;  
OneWayANOVA  
GroupMeans = .4 | .6 | 0  
Stddev =1  
GroupWeights = ( 1 1 1 ) ( 2 2 1 )  
Test =Contrast  
Alpha =.05  
Ntotal = 90  
Power = .  
Contrast = ( -1 -1 2 ) (-1 1 0 );  
PLOT X =N Min = 30 Max = 180  
Key =OnCurves;  
RUN;
```

One way Anova

3 Means =.4 .6 0.0

Two weighting schemes

TWO contrasts

**Show
results**

Proc Power: OneWayAnova

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The POWER Procedure

Single DF Contrast in One-Way ANOVA

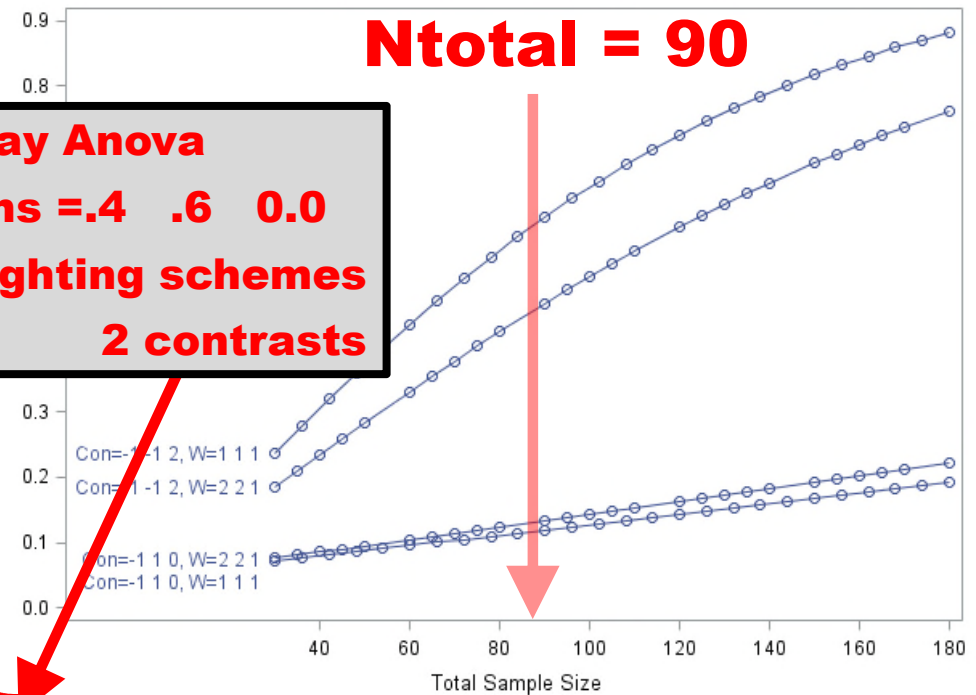
Fixed Scenario Elements

| | |
|---------------------|-----------|
| Method | Exact |
| Alpha | 0.05 |
| Group Means | 0.4 0.6 0 |
| Standard Deviation | 1 |
| Total Sample Size | 90 |
| Number of Sides | 2 |
| Null Contrast Value | 0 |

Power to Detect Range of Specific Between-Group Mean Differences

Will calculate power for sample sizes around Ntotal

Single DF Contrast in One-Way ANOVA



One way Anova
3 Means = .4 .6 0.0
2 weighting schemes
2 contrasts

Computed Power

| Index | Contrast | | | Weights | | | Power |
|-------|----------|----|---|---------|---|---|-------|
| 1 | -1 | -1 | 2 | 1 | 1 | 1 | 0.599 |
| 2 | -1 | -1 | 2 | 2 | 2 | 1 | 0.467 |
| 3 | -1 | 1 | 0 | 1 | 1 | 1 | 0.119 |
| 4 | -1 | 1 | 0 | 2 | 2 | 1 | 0.134 |

McNemar Exact Conditional Test

```
PROC Power; PairedFreq  
dist=exact_cond  
discproportions = 0.15 | 0.45  
npairs = 80 power = .; run;
```

difference and sum of discordant proportions

```
PROC Power; PairedFreq  
dist=exact_cond  
discpropdiff = 0.3  
totalpropdisc = 0.6  
npairs = 80 power = .; run
```

McNemar Normal Approx. Test

```
PROC Power; PairedFreq  
dist=normal method=connor  
discproportions = 0.15 | 0.45  
npairs = . power = .9; Run;
```

You can also **express effects** in terms of:

- 1) the difference of discordant proportions and the reference discordant proportion:
- 2) the ratio of discordant proportions and the denominator of the ratio
- 3) the ratio and sum of discordant proportions
- 4) the paired proportions and correlation
- 5) proportion difference, reference proportion, and correlation
- 6) the odds ratio, reference proportion, and correlation:
- 7) relative risk, reference proportion, and correlation

/* Paired T test*/

PROC Power; PairedMeans

test=diff

meandiff = 7

corr = 0.4

stddev = 12

npairs = 50

power = . ;

run;

**/* Additive Equivalence Test for Mean
Difference with Normal Data*/**

PROC Power; PairedMeans

test=equiv_diff

lower = 2 upper = 5 meandiff = 4

corr = 0.2

stddev = 8

npairs = .

power = 0.9;

Run;

/* Multiplicative Equivalence Test - Mean Ratio w/ Lognormal Data*/

PROC Power; PairedMeans

test=equiv_ratio

lower = 3 upper = 7

meanratio = 5

cv = 1.1

corr = 0.2

npairs = 50

power = . ; run;

/* Confidence Int. for Mean Difference*/

PROC Power; PairedMeans

ci = diff

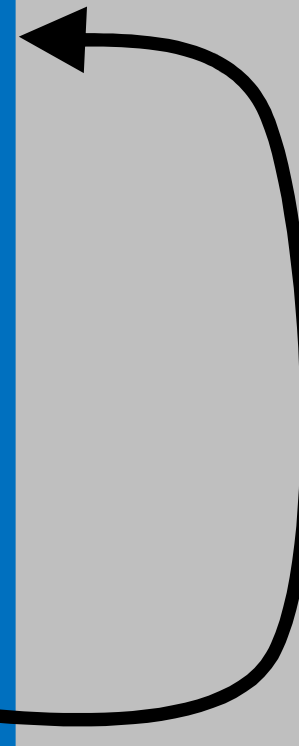
halfwidth = 4

corr = 0.35

stddev = 8

npairs = 30

probwidth = . ;; run;



Options within PairedMeans for PROC POWER:

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

TEST = Diff provides test of mean difference

PairedMeans = Means to be tested for difference

PairedStddevs = Measure-specific SD for means to be tested

Stddev = Common SD for means to be tested

MeanDiff = Mean difference to be tested

Corr = correlations between measures

TITLE1 "Power to Detect Range of Repeated Measures Mean Differences";

TITLE2 "Will calculate power for sample sizes around Npairs";

PROC POWER; **PairedMeans**

MeanDiff = .2 .4 .6

Stddev = 1

Corr = .3 .7

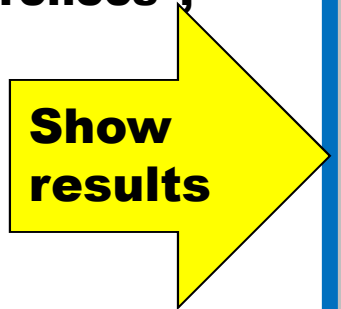
Alpha = .05

Npairs = 25

Power = . ;

PLOT X =N Min = 10 Max = 50 **Key=OnCurves** **VarY(Panel BY Corr);**

RUN ;



**Show
results**

Options within PairedMeans for PROC POWER:

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The POWER Procedure Paired t Test for Mean Difference

Power to Detect Range of Repeated Measures Mean Differences

Will calculate power for sample sizes around Npairs

Fixed Scenario Elements

| | |
|--------------------|--------|
| Distribution | Normal |
| Method | Exact |
| Alpha | 0.05 |
| Standard Deviation | 1 |
| Number of Pairs | 25 |
| Number of Sides | 2 |
| Null Difference | 0 |

**Calculate
power for
sample sizes
around Npairs**

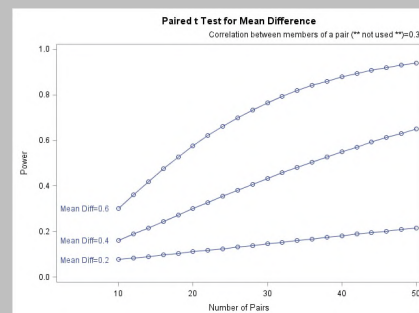
**3 Mean diff
2 Correlations**

Corr = .3 .7

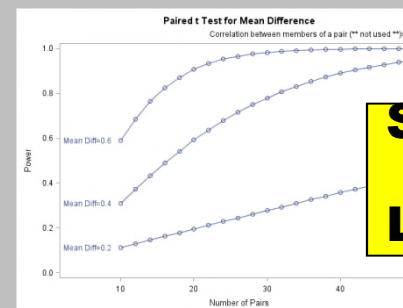
Computed Power

| Index | Mean Diff | Corr | Power |
|-------|-----------|------|-------|
| 1 | 0.2 | 0.3 | 0.128 |
| 2 | 0.2 | 0.7 | 0.236 |
| 3 | 0.4 | 0.3 | 0.368 |
| 4 | 0.4 | 0.7 | 0.698 |
| 5 | 0.6 | 0.3 | 0.682 |
| 6 | 0.6 | 0.7 | 0.960 |

PLOT X =N Min = 10 Max = 50 Key=OnCurves VarY(Panel BY Corr);



6 plots



**Show
LARGER**

Options within PairedMeans for PROC POWER:

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

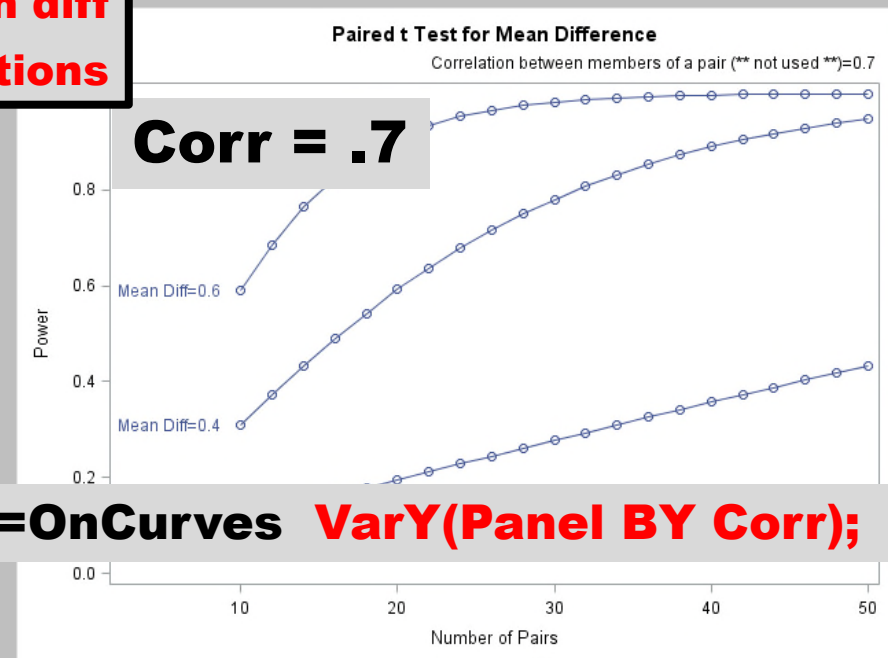
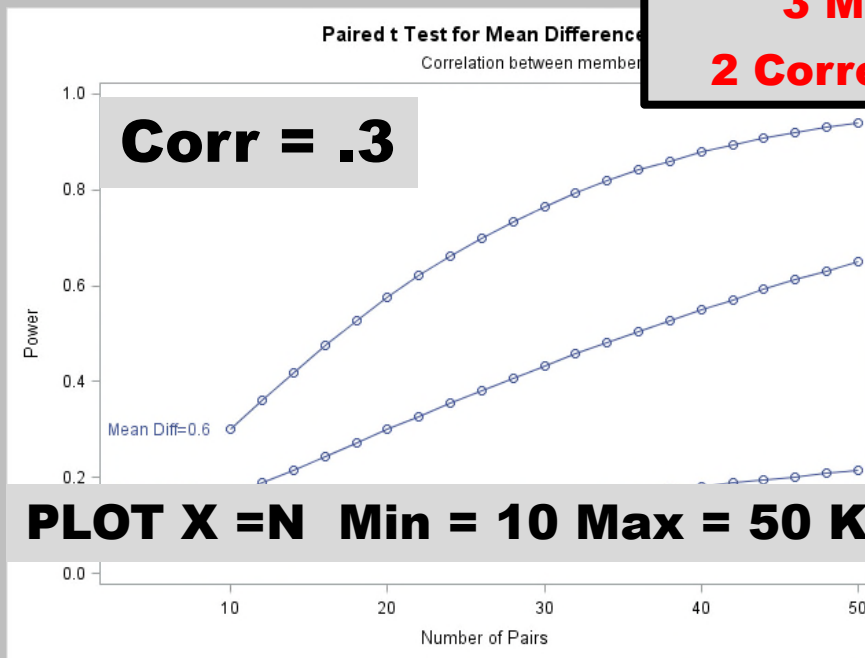
The POWER Procedure Paired t Test for Mean Difference

Power to Detect Range of Repeated Measures Mean Differences

Will calculate power for sample sizes around Npairs

Calculate
power for
sample sizes
around Npairs

3 Mean diff
2 Correlations



PLOT X =N Min = 10 Max = 50 Key=OnCurves VarY(Panel BY Corr);

**/* BALANCED Pearson Chi-Square
Test for Two Proportions*/**

PROC Power; TwoSampleFreq

test=pchi

groupproportions = (.15 .25)

nullproportiondiff = .03

npergroup = 50

power = .;

run;

**/* UN BALANCED Pearson Chi-
Square Test for Two Proportions*/**

PROC Power; TwoSampleFreq

test=pchi

oddsratio = 2.5

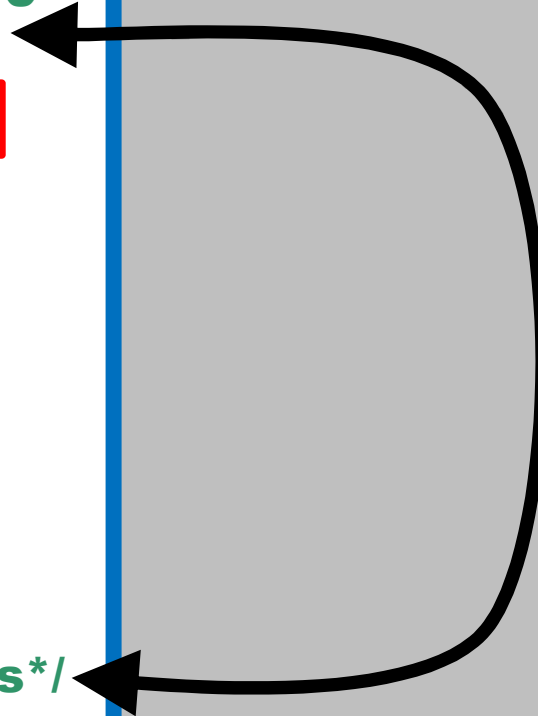
refproportion = 0.3

groupweights = (1 2)

ntotal = .

power = 0.8;

run;

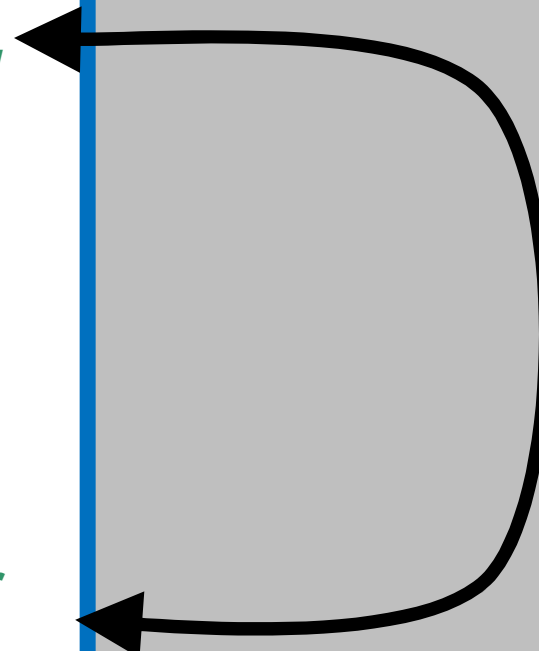


```
/* UNBALANCED Pearson Chi-Square Test  
for Two Proportions Groupn and rel risk*/
```

```
PROC Power; TwoSampleFreq  
test=pchi  
relativerisk = 1.5 refproportion = 0.2  
groupns = 40 | 60  
power = . ;  
run;
```

```
/* BALANCED Pearson Chi-Square Test for  
Two Proportions ProportionDiff*/
```

```
PROC Power; TwoSampleFreq  
test=pchi  
proportiondiff = 0.15 refproportion = 0.4  
ntotal = 100  
power = . ;  
run;
```

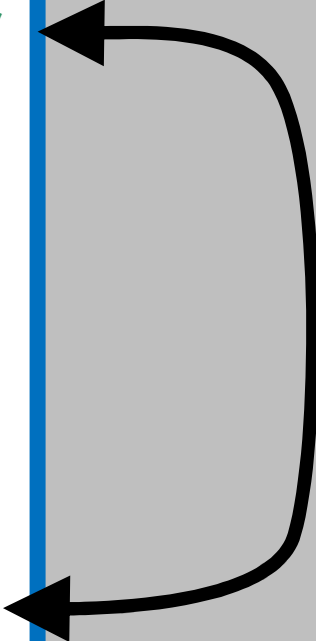


Fisher's Exact Conditional Test for Two Proportions

```
PROC Power; TwoSampleFreq  
test=fisher  
groupproportions = (.35 .15)  
npergroup = 50  
power = .;  
run;
```

Likelihood Ratio Chi-Square Test for Two Proportions

```
PROC Power; TwoSampleFreq  
test=lrchi  
oddsratio = 2 refproportion = 0.4  
npergroup = .  
power = 0.9;  
run;
```

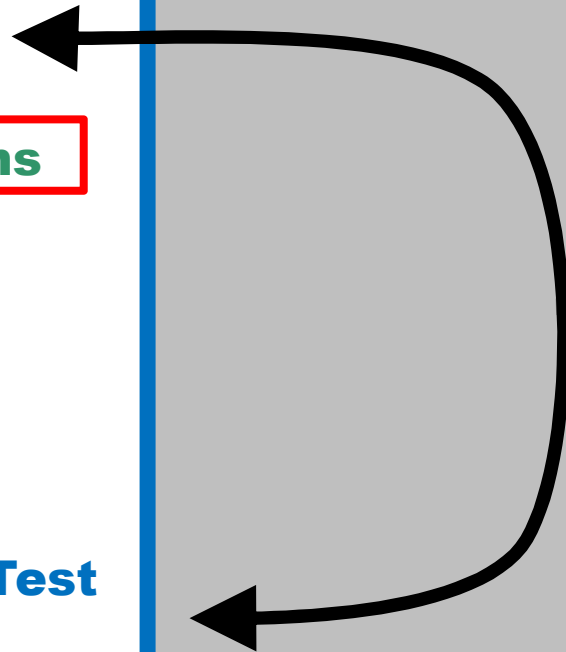


Balanced Two-Sample T Test
Assuming Equal Variances

```
PROC Power; TwoSampleMeans  
test=diff  
meandiff = 7  
stddev = 12  
npergroup = 50  
power = . ;  
run;
```

UNBALANCED Two-Sample T Test
Assuming Equal Variances

```
PROC Power; TwoSampleMeans  
test=diff  
groupmeans = 8 | 15  
groupweights = (2 3)  
stddev = 4  
ntotal = .  
power = 0.9;  
run;
```

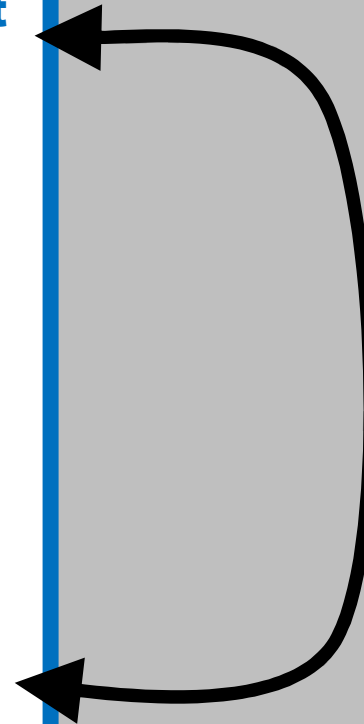


Two-Sample Satterthwaite T Test Assuming Unequal Variances

```
PROC Power; TwoSampleMeans  
test=diff_satt  
meandiff = 3  
groupstddevs = 5 | 8  
groupweights = (1 2)  
ntotal = 60  
power = . ;  
run;
```

Two-Sample Pooled T Test of Mean Ratio with Lognormal Data

```
PROC Power; TwoSampleMeans  
test=ratio  
meanratio = 7  
cv = 0.8  
groupns = 50 | 70  
power = . ;  
run;
```

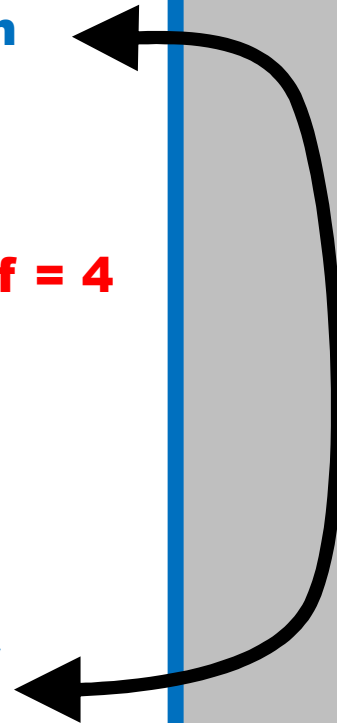


Additive Equivalence Test for Mean Difference with Normal Data

```
PROC Power; TwoSampleMeans  
test=equiv_diff  
lower = 2      upper = 5    meandiff = 4  
stddev = 8  
ntotal = .  
power = 0.9;  
run;
```

Multiplicative Equivalence Test for Mean Ratio with Lognormal Data

```
PROC Power; TwoSampleMeans  
test=equiv_ratio  
lower = 3    upper = 7    meanratio = 5  
cv = 0.75  
npergroup = 50  
power = .;  
run;
```



Confidence Interval for Mean Difference

PROC Power; TwoSampleMeans

ci = diff

halfwidth = 4

stddev = 8

groupns = (30 35)

probwidth = .;

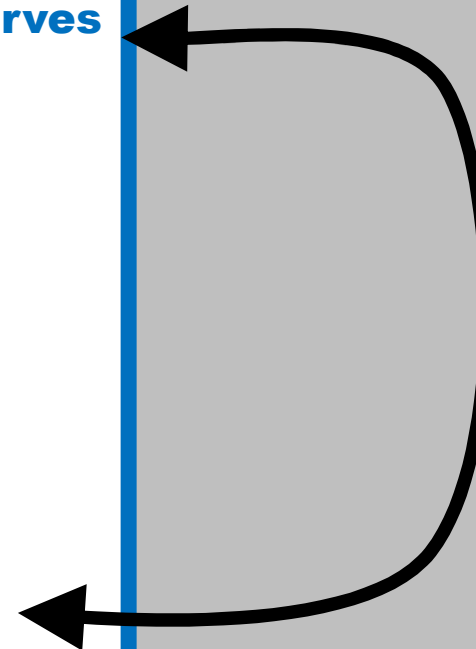
run;

Balanced Log-Rank Test Two Survival Curves

```
PROC Power: TwoSampleSurvival  
test=logrank  
curve("Control") = (1 2 3):(0.8 0.7 0.6)  
curve("Treatment") = (5):(.6)  
groupsurvival = "Control" | "Treatment"  
accrualtime = 2  
followuptime = 1  
npergroup = 50  
Power = . ; run;
```

UNBalanced Log-Rank Test-Two Survival Curves

```
PROC Power: TwoSampleSurvival  
test=logrank  
curve("Control") = (1 2 3):(0.8 0.7 0.6)  
refsurvival = "Control"  
hazardratio = 1.5  
accrualtime = 2  
followuptime = 1  
groupweights = (1 2)  
ntotal = .  
power = 0.8; run;
```



Calc. accrual rate using ACCRUALRATETOTAL=

PROC Power; TwoSampleSurvival

test=logrank

curve("Control") = (1 2 3):(0.8 0.7 0.6)

refsurvival = "Control"

hazardratio = 1.5

accrualtime = 2

followuptime = 1

groupweights = (1 2)

accrualratetotal = .

power = 0.8; run;

Calc. expected # of events

PROC Power; TwoSampleSurvival

test=logrank

curve("Control") = (1 2 3):(0.8 0.7 0.6)

refsurvival = "Control"

hazardratio = 1.5

accrualtime = 2

followuptime = 1

groupweights = (1 2)

eventstotal = .

power = 0.8; run;

specify sample n with the **GROUPNS=** and specify exp. survival curves in terms of **median survival times**

PROC Power; TwoSampleSurvival

test = logrank

groupmedsurvtimes = (16 22)

accrualtime = 6 totaltime = 18

groupns = 40 | 60

power = .;

Specify exp. survival curves using **hazard ratio and reference hazard.**

PROC Power; TwoSampleSurvival

test = logrank

hazardratio = 1.2 refsurvexphazard = 0.7

accrualtime = 2 totaltime = 4

ntotal = 100

power = .;

run;

You can also specify exponential survival curves in terms of the individual hazards, as in the following statements:

```
PROC Power; TwoSampleSurvival  
test = logrank
```

```
groupsurvexphazards = 0.7 | 0.84
```

```
accrualtime = 2
```

```
totaltime = 4
```

```
ntotal = .
```

```
power = 0.9;
```

```
run;
```

Gehan Rank Test for Two Survival Curves

PROC Power; TwoSampleSurvival

test = Gehan

groupmedsurvtimes = 5 | 7

accrualtime = 3 totaltime = 6

npergroup = .

power = 0.8;

run;

Tarone-Ware Rank Test--2 Survival Curves

PROC Power; TwoSampleSurvival

test = TaroneWare

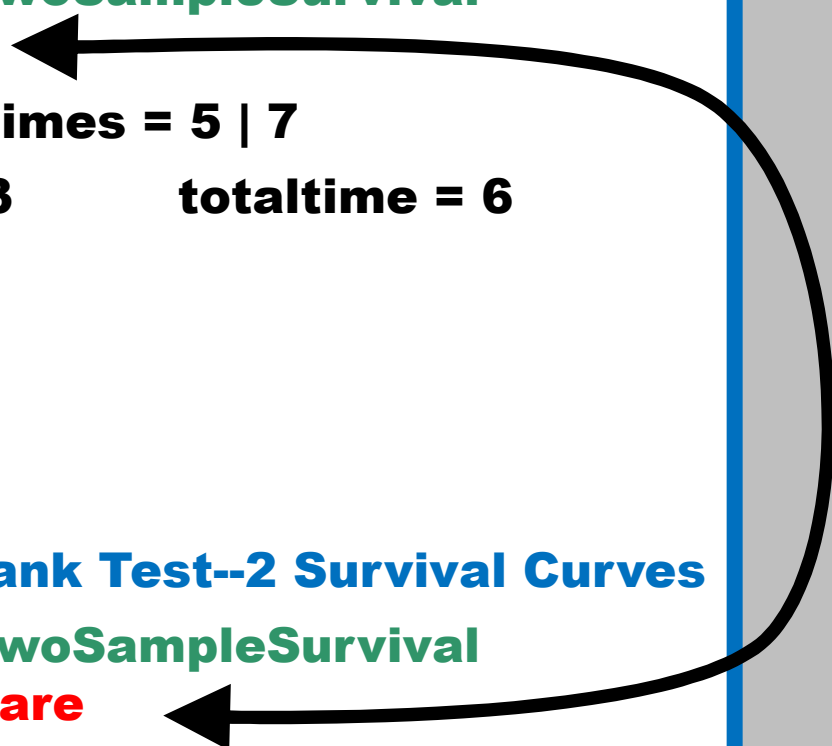
groupmedsurvtimes = 5 | 7

accrualtime = 3 totaltime = 6

npergroup = 100

power = .;

run;



Proc Power: TwoSampleWilcoxon

```
vardist("myordinal") = ordinal ((0 1 2) : (.2 .3 .5))  
vardist("mybeta1") = beta (1, 2)  
vardist("mybeta2") = beta (1, 2, 0, 2)  
vardist("mybinomial") = binomial (.3, 3)  
vardist("myexponential") = exponential (2)  
vardist("mygamma") = gamma (1.5, 2)  
vardist("mylaplace") = laplace (1, 2)  
vardist("mylogistic") = logistic (1, 2)  
vardist("mylognormal") = lognormal (1, 2)  
vardist("mynormal") = normal (3, 2)  
vardist("mypoisson") = poisson (2)  
vardist("myuniform") = uniform (0, 2)  
variables = "myordinal" | "mybeta1" "mybeta2" "mybinomial"  
"myexponential" "mygamma" "mylaplace"  
"mylogistic" "mylognormal" "mynormal"  
"mypoisson" "myuniform"  
ntotal = 40  
power = . ; run;
```



**Show
results**

The POWER Procedure
Wilcoxon-Mann-Whitney
Test

Fixed Scenario Elements

| | |
|--------------------------|---|
| Method | O'Brien-Castellote approximation |
| Total Sample Size | 40 |
| Number of Sides | 2 |
| Alpha | 0.05 |
| Group 1 Weight | 1 |
| Group 2 Weight | 1 |
| NBins Per Group | 1000 |

Computed Power

| Index | Variables | | Pooled N Bins | Power |
|--------------|------------------|----------------------|----------------------|--------------|
| 1 | myordinal | mybeta1 | 1003 | 0.887 |
| 2 | myordinal | mybeta2 | 1002 | 0.718 |
| 3 | myordinal | mybinomial | 5 | 0.404 |
| 4 | myordinal | myexponential | 1003 | 0.132 |
| 5 | myordinal | mygamma | 1003 | 0.741 |
| 6 | myordinal | mylaplace | 1002 | 0.124 |
| 7 | myordinal | mylogistic | 1002 | 0.103 |
| 8 | myordinal | mylognormal | 1003 | 0.578 |
| 9 | myordinal | mynormal | 1003 | 0.894 |
| 10 | myordinal | mypoison | 10 | 0.359 |
| 11 | myordinal | myuniform | 1002 | 0.413 |

PROC GLMPower

Examples from the Web

SAS Documentation

SUG papers &

Academic web pages

PROC GLMPower Syntax

The GLMPower procedure performs prospective power analysis for general linear models. The procedure supports:

Type III tests and contrasts of fixed class effects

continuous and categorical covariates

unbalanced designs

customized graphics.

PROC GLMPower requires an exemplary data set that is used to pass parameters to PROC GLMPower.

- 1) The Input data set will contain:**
- 2) Population response means**
- 3) Design weights (If unbalanced design)**

multiple scenarios can be simulated in one PROC GLMPower call.

```
PROC GLMPower <options>;  
CLASS variables;  
MODEL dependent-variables =  
      classification-effects;  
WEIGHT variable;  
CONTRAST 'label' effect  
      values<...effectvalues></options>;  
POWER <options>;  
PLOT<plot-options></graph-options>;  
RUN;
```



PROC GLMPower Syntax

X variables can be categorical, continuous or a mixture of both.

Each Y variable must point to a set of cell averages in the data

Multiple Y variables can be processed in one proc

Main effects and interactions are modeled in a manner similar to GLM

You can model the effect of covariates with:

the NCOVARIATES= option and **one of** the

1) CORRXY= or

2) PROPVARREDUCTION= options

There are **other** syntax limitations/Quirks:

The class statement appears above the Model statement.

The MODEL statement appears above the POWER statement.



```
Data bp;
input treat$ reduce cellwgt @@;
Datalines;
1placebo 5 1 2standard 12 1
3Newlow 10.5 1 4Newhigh 13.5 1;
run;
```

```
PROC GLMPower data=bp data=order;
class treat;
model reduce=treat;
weight cellwgt;
contrast 'placebo vs. low' treat 10-10;
contrast 'placebo vs. high' treat 100-1;
contrast 'standard vs. low' treat 01-10;
contrast 'standard vs. high' treat 010-1;
power
stddev=6 alpha=0.0125 ntotal = .
power=0.9;
PLOT X=power Min=.1 Max=.95
Key=OnCurves; run;
```

We wish to compare the reduction in blood pressure resulting from use of a placebo, a standard drug and a new drug at both a low dose and a high dose. Previous studies with the standard drug suggest a standard deviation of about 6 mmHg.

In the past the placebo has resulted in reductions of about 5mmHg and the standard drug of about 12mmHg.

The researcher guesses the low dose new drug will result in a reduction of about 10.5 mmHg and the high dose will result in a reduction of about 13.5 mmHg.

Show results



The GLMPOWER Procedure

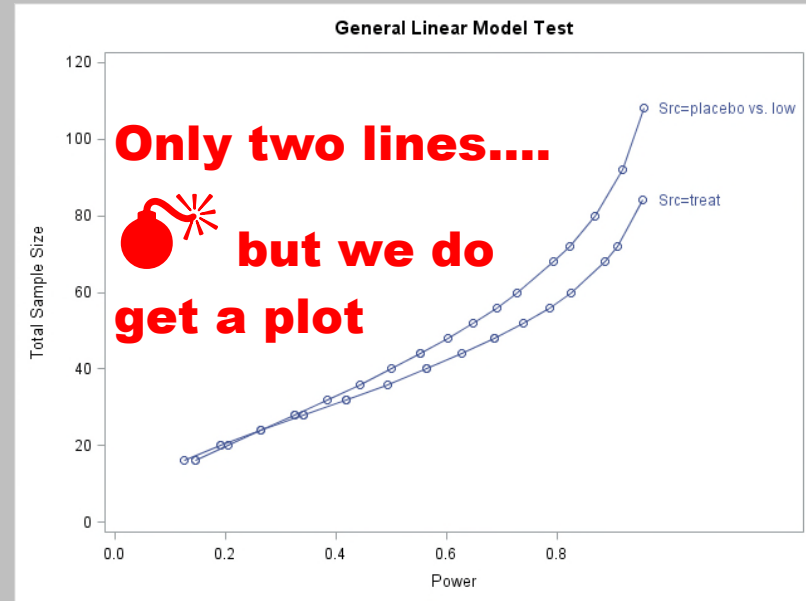
Fixed Scenario Elements

| | |
|--------------------------|---------|
| Dependent Variable | reduce |
| Weight Variable | cellwgt |
| Alpha | 0.0125 |
| Error Standard Deviation | 6 |
| Nominal Power | 0.9 |

Computed N Total

| Index | Type | Source | Test DF | Error DF | Actual Power | N Total | Error |
|-------|----------|-------------------|---------|----------|--------------|---------|-------------|
| 1 | Effect | treat | 3 | 68 | 0.909 | 72 | |
| 2 | Contrast | placebo vs. low | 1 | 84 | 0.903 | 88 | |
| 3 | Contrast | placebo vs. high | . | . | . | . | Inestimable |
| 4 | Contrast | standard vs. low | . | . | . | . | Inestimable |
| 5 | Contrast | standard vs. high | . | . | . | . | Inestimable |

http://familymed.uthscsa.edu/research08/pcrmisc/2014h_2005/presentations/5.%20Sample%20Size%20and%20Power,%20John%20Boltri%20MD,%20Cindy%20Passmore%20MS,%20Robert%20L%20Vogel%20PhD.pdf



```

Data Pain;
input Treatment $
      PainMem0    PainMem1Wk
      PainMem6Mo PainMem12Mo;
datalines;
SensoryFocus  2.40  2.38  2.05  1.90
StandardOfCare 2.40  2.39  2.36  2.30;
Run;

```

Repeated Measures

```

ods graphics on;
PROC GLMPOWER data=Pain;
CLASS Treatment;
MODEL PainMem0 PainMem1Wk PainMem6Mo
      PainMem12Mo = Treatment;
repeated Time contrast;
POWER mtest = hlt alpha = 0.01
      power = .9      ntotal = .
      StdDev = 0.92 1.04
Matrix ("PainCorr") =
      lear(0.6, 0.8, 4, 0 1 26 52)
CorrMat = "PainCorr";
PLOT y=power min=0.05 max=0.99
      yopts=(ref=0.9) vary (linestyle by stddev,
      symbol by dependent source); run;
ods graphics off;

```

Logan, Baron, and Kohout (1995) and Guo et al. (2013) study a dental intervention on the memory of pain.

The study compare sensory focus to standard care over a period of a year, asking patients to **self-report immediately after** the procedure and then again at **1 week, 6 , and 12 months**.

The correlation is thought to be linear exponent autoregressive (LEAR), with a **correlation of about 0.6** and a **decay rate of about 0.8** over one-week intervals. X has 2 levels (sensory focus versus standard care), and you allocate to a balanced design.

The within-subject factor is time, with four levels (0, 1, 26, and 52 weeks).

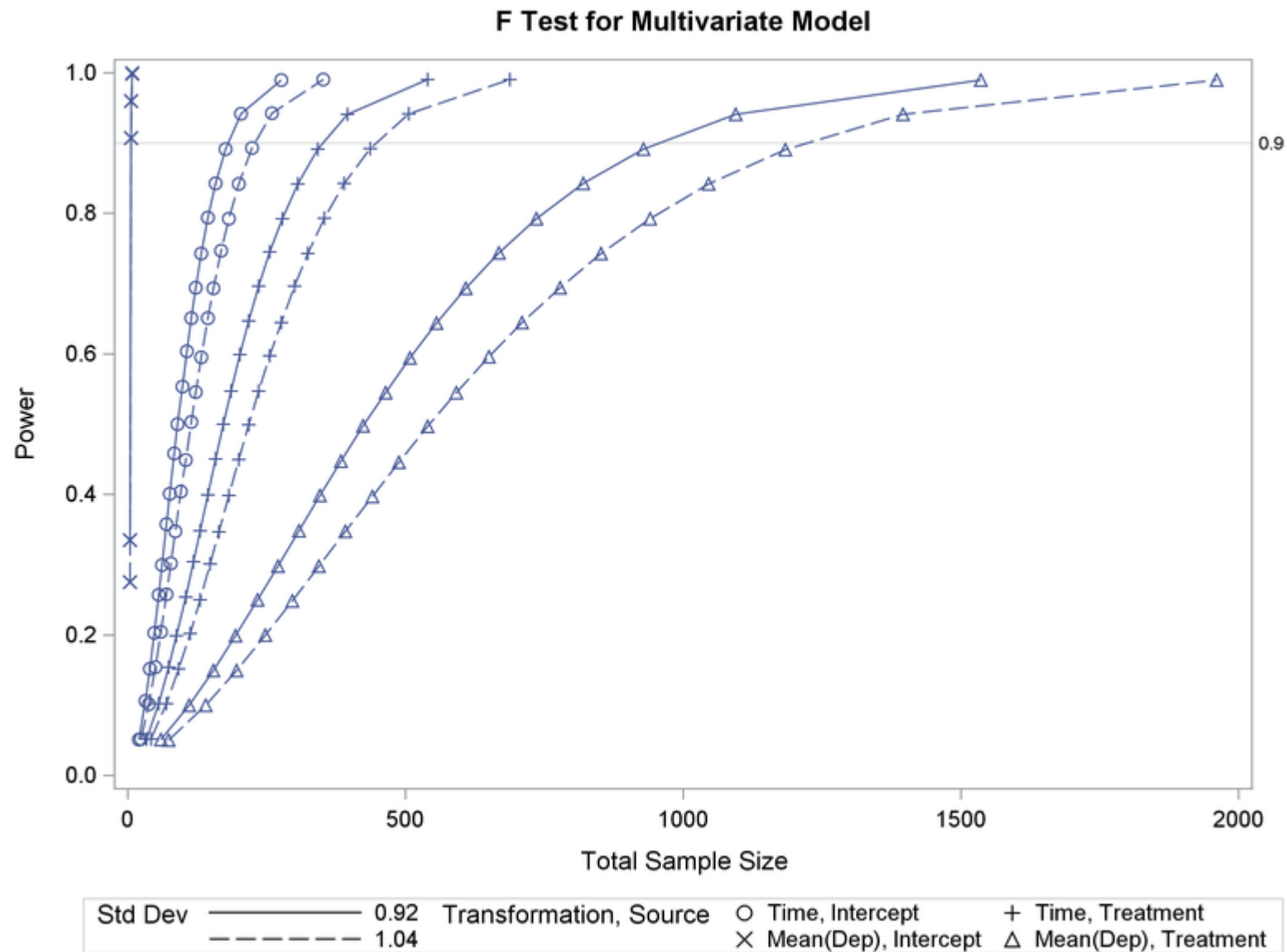
Show results

Table 47.14: Conjectured Correlation Matrix

| Time (week) | 0 | 1 | 26 | 52 |
|--------------------|--------------|--------------|--------------|--------------|
| 0 | 1 | 0.6 | 0.491 | 0.399 |
| 1 | 0.6 | 1 | 0.495 | 0.402 |
| 26 | 0.491 | 0.495 | 1 | 0.491 |
| 52 | 0.399 | 0.402 | 0.491 | 1 |

Computed N Total

| Index | Transformation | Source | Std Dev | Effect | Num DF | Den DF | Actual Power | N Total |
|--------------|-----------------------|------------------|----------------|----------------------------|---------------|---------------|---------------------|----------------|
| 1 | Time | Intercept | 0.92 | Time | 3 | 176 | 0.90 | 180 |
| 2 | Time | Intercept | 1.04 | Time | 3 | 226 | 0.90 | 230 |
| 3 | Time | Treatment | 0.92 | Time* Treatment | 3 | 346 | 0.90 | 350 |
| 4 | Time | Treatment | 1.04 | Time* Treatment | 3 | 442 | 0.90 | 446 |
| 5 | Mean(Dep) | Intercept | 0.92 | Intercept | 1 | 4 | 0.96 | 6 |
| 6 | Mean(Dep) | Intercept | 1.04 | Intercept | 1 | 4 | 0.90 | 6 |
| 7 | Mean(Dep) | Treatment | 0.92 | Treatment | 1 | 950 | 0.90 | 952 |
| 8 | Mean(Dep) | Treatment | 1.04 | Treatment | 1 | 1214 | 0.90 | 1216 |



Stat 582

**☹ Throws Error
but message
is not the
most helpful**

```
Data Fluids;
INFILE DATALINES FIRSTOBS=2;
input @1 Fluid $CHAR5. @7 LacticAcid1 @14 LacticAcid2 @23 CellWgt;
datalines;
```

```
123456789012345678901234567890
```

```
Water 35.6 35.6 2
```

```
A1 33.7 33.7 1
```

```
A2 30.2 30.2 1
```

```
B1 29 28 1 ☹ Throws
```

```
B2 25.9 25.9 1 Error
```

```
;
```

*/*Then the SAS code for the power analysis
with standard deviation=3.75
alpha=0.025 and power=0.9 is:*/*

```
PROC GLMPower data =Fluids;
```

```
Class Fluid;
```

```
weight CellWgt;
```

```
Model Fluid = LacticAcid1 LacticAcid2;
```

```
power stddev =3.75
```

```
alpha=0.025
```

```
ntotal=.
```

```
power=0.9;
```

```
run;
```

```
quit;
```

```
16 PROC GLMPower data =Fluids;
```

```
17 Class Fluid;
```

```
18 weight CellWgt;
```

```
19 Model Fluid = LacticAcid1 LacticAcid2;
```

**ERROR: Variable Fluid in list does not match
type prescribed for this list.**

**NOTE: The previous statement has been
deleted.**

```
20 power stddev =3.75
```

```
21 alpha=0.025
```

```
22 ntotal=.
```

```
23 power=0.9;
```

```
24 run;
```

Cuckoo egg Power examples
Complex and Cool Examples
that compare
different methods of calculating power
and show how
Group means , in ANOVA, affect power

Cuckoo Power examples

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

/* There are 6 host species in whose nests cuckoo birds lay eggs. What sample size is needed to detect a difference between 21 and 23 mm. The standard deviation is about 1 mm. */

Compute power curves for a single factor CRD ANOVA */

Power computations will be done using three procedures –

Proc Power: suitable for simple designs –

Proc GLMPower: suitable for more complex designs with a single error term allowing for covariates etc. –

Methods of Stroup: suitable for ALL design (including those with multiple error terms)

SAS also has an interactive program to compute power - look in your SAS directory under the START button in WinDoze */ dm 'output' clear; dm 'log' clear;

Cuckoo Power examples

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

5 examples form the same research project

All are ANOVA problems with 6 Classes/Levels of X

PROC Power

with two different sets of means

PROC GLMPower

with the same two sets of means

Stroup's method

Ex #1 Means are: 21 22 22 22 22 23

Worst configuration of means – Hardest to detect

Ex #2 Means are: 21 21 21 23 23 23

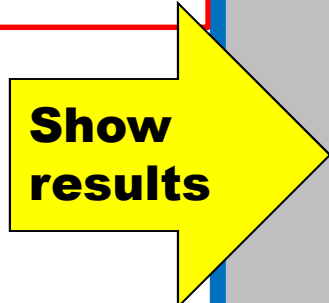
Best configuration of means – Easiest to detect

Cuckoo Ex. #1

Proc Power Hard to detect

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
options orientation=landscape; ods
pdf file='E:\___Proc_power\cuckoo-power.pdf';
goptions device=pdf colors=(black) rotate=landscape;
title 'Cuckoo egg size power analysis';
options nodate noovp;
%let alpha=.05; %let power=.80; %let stddev= 1;
%let var=%sysevalf(&stddev*&stddev); /*←compute variance */
PROC POWER; title2 'Using a base difference of 2 mm';
onewayanova
groupmeans = 21 | 22 | 22 | 22 | 22 | 23 /* list group means*/
stddev = &stddev /* what is the standard deviation */
alpha = &alpha /* what is the alpha level */
power = &power /* target power */
ntotal = . /* solve for TOTAL samplesize */ ;
/* end of the onewayanova statement - don't forget it */
plot y=power yopts=(ref=.80 crossref=yes) min=.05 max=.95;
footnote 'This configuration has the worst power and so the largest
possible sample size'; run;
```



Show
results

Cuckoo Ex. #1

Proc Power Hard to detect

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

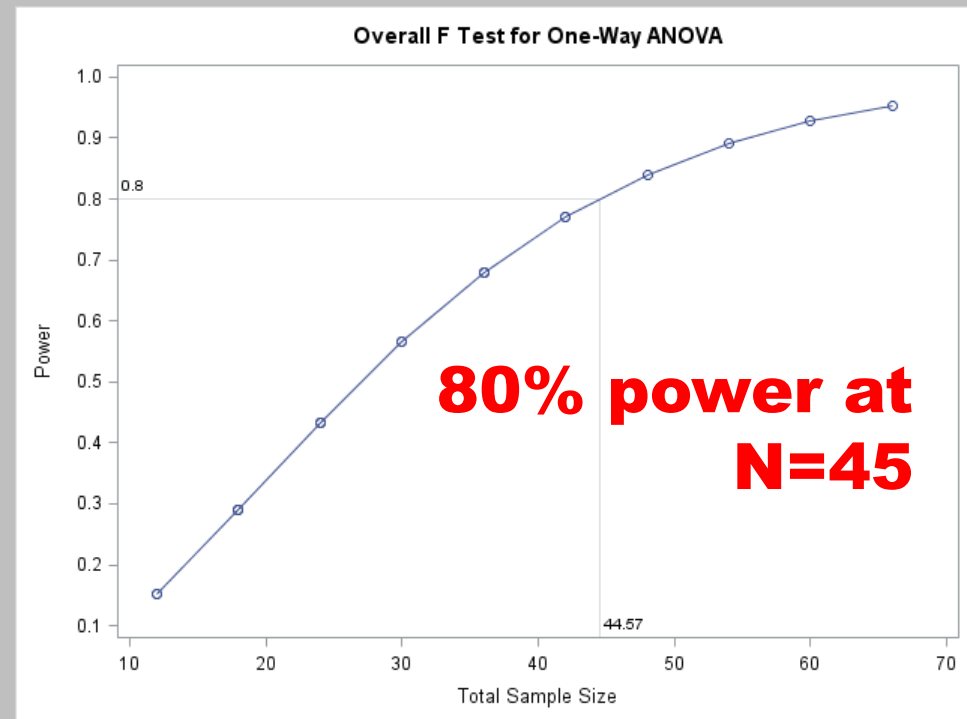
The POWER Procedure
Overall F Test for One-Way
ANOVA

Fixed Scenario Elements

| | |
|--------------------|-------------------|
| Method | Exact |
| Alpha | 0.05 |
| Group Means | 21 22 22 22 22 23 |
| Standard Deviation | 1 |
| Nominal Power | 0.8 |
| Group Weights | 1 1 1 1 1 1 |

Computed N Total

| | |
|--------------|---------|
| Actual Power | N Total |
| 0.840 | 48 |




Cuckoo Ex. #2

Proc Power Easy to detect

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
proc power;  
title2 'Using a base difference of 2 mm with a different configuration  
of means';  
onewayanova groupmeans=21| 21| 21| 23| 23| 23/*list group means*/  
stddev = &stddev /* what is the standard deviation */  
alpha = &alpha /* what is the alpha level */  
power = &power /* target power */  
ntotal = . /* solve for TOTAL sample size */ ;  
/* end of the onewayanova statement - don't forget it */  
plot y=power yopts=(ref=.80 crossref=yes) min=.05 max=.95;;  
footnote 'This configuration has the best power and so the smallest  
possible sample size'; run;
```



Show
results

Cuckoo Ex. #2

Proc Power Easy to detect

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

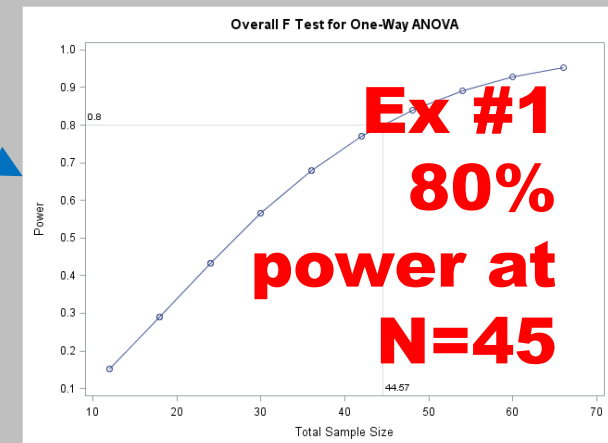
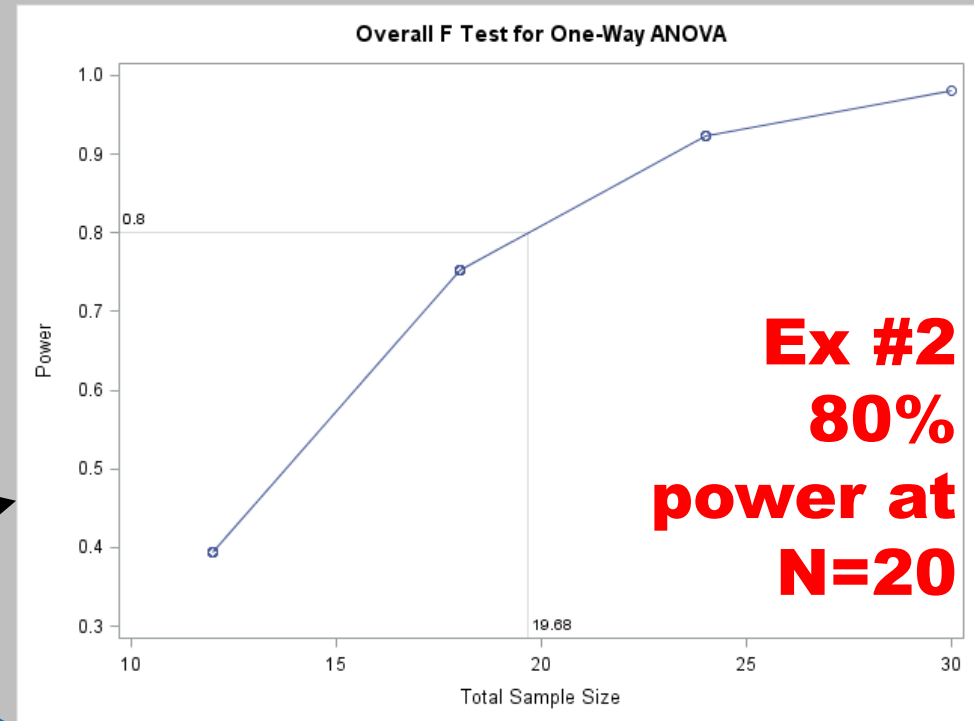
The POWER Procedure
Overall F Test for One-Way
ANOVA

Fixed Scenario Elements

| | |
|--------------------|--|
| Method | Exact |
| Alpha | 0.05 |
| Group Means | 21 21 21 23 23 23 Ex #1 Means were 21 22 22 22 22 23 |
| Standard Deviation | 1 |
| Nominal Power | 0.8 |
| Group Weights | 1 1 1 1 1 1 |

Computed N Total

| | |
|--------------|---------|
| Actual Power | N Total |
| 0.923 | 24 |



Cuckoo Ex. #3

Proc GLMPower Hard to detect

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
data means;  
infile datalines ;  
input species $ mean_set1 mean_set2 @@;  
datalines;
```

```
s1 21 21 s2 22 21 s3 22 21 s4 22 23 s5 22 23 s6 23 23
```

```
;run;
```

```
proc glmpower data=means;  
title2 'GLMPower - Worst configuration of means';  
class species;  
model mean_set1 = species;
```


```
power stddev = &stddev
```

```
alpha = &alpha
```

```
ntotal = .
```

```
power = &power;
```

```
plot y=power yopts=(ref=.80 crossref=yes) min=.05 max=.95;; run;
```



Show
results

Cuckoo Ex. #3

Proc GLMPower Hard to detect

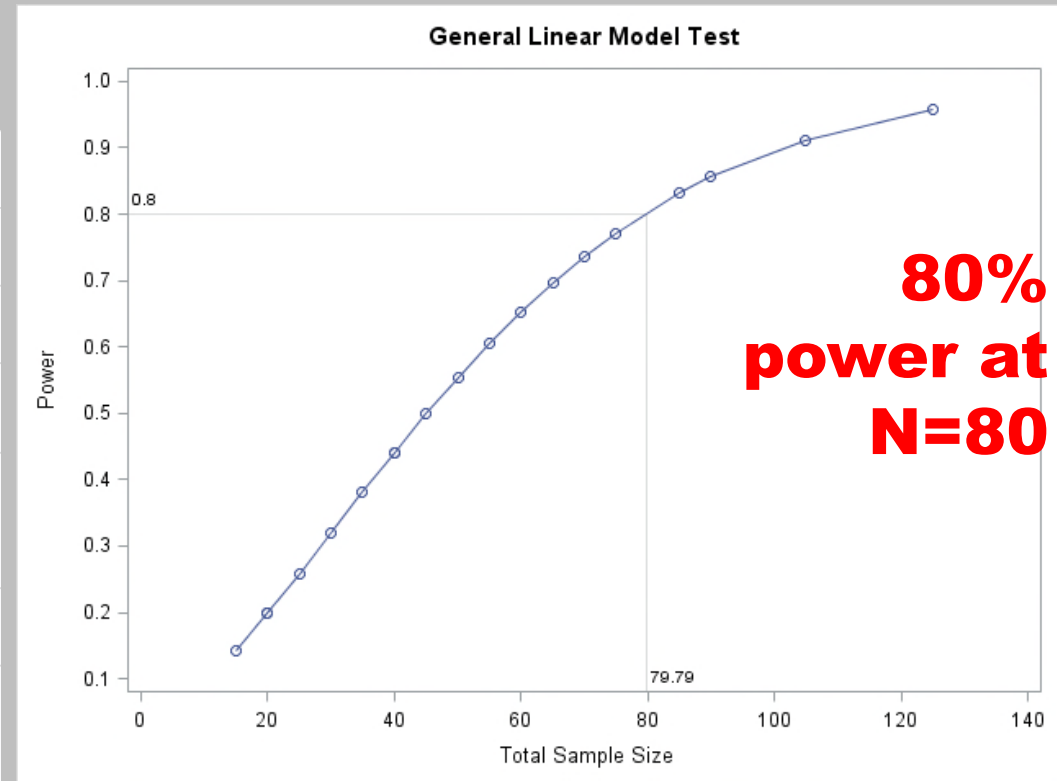
<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

Fixed Scenario Elements

| | |
|--------------------------|-----------|
| Dependent Variable | mean_set1 |
| Source | species |
| Alpha | 0.05 |
| Error Standard Deviation | 1 |
| Nominal Power | 0.8 |
| Test Degrees of Freedom | 4 |

Computed N Total

| Error DF | Actual Power | N Total |
|----------|--------------|---------|
| 75 | 0.803 | 80 |



Cuckoo Ex. 4

Proc GLMPower Easy to detect

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
data means;
infile datalines ;
input species $ mean_set1 mean_set2 @@;
datalines;
s1 21 21 s2 22 21 s3 22 21 s4 22 23 s5 22 23 s6 23 23
;run;
proc glmpower data=means;
title2 'GLMPower - Best configuration of means';
class species;
model mean_set2 = species;
power stddev = &stddev
      alpha = &alpha
      ntotal = .
      power = &power;
plot y=power yopts=(ref=.80 crossref=yes) min=.05 max=.95;; run;
```



Show
results

Cuckoo Ex. 4

Proc GLMPower Easy to detect

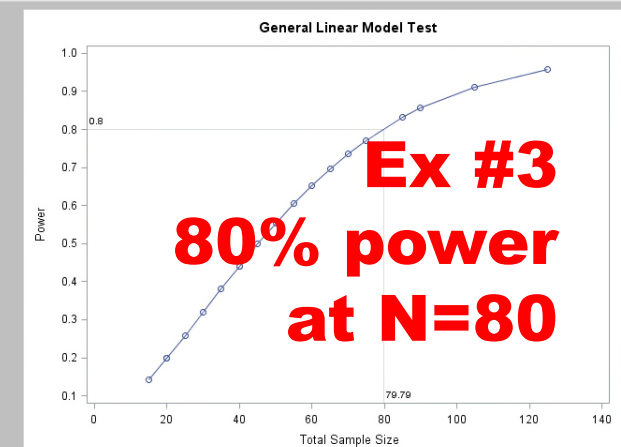
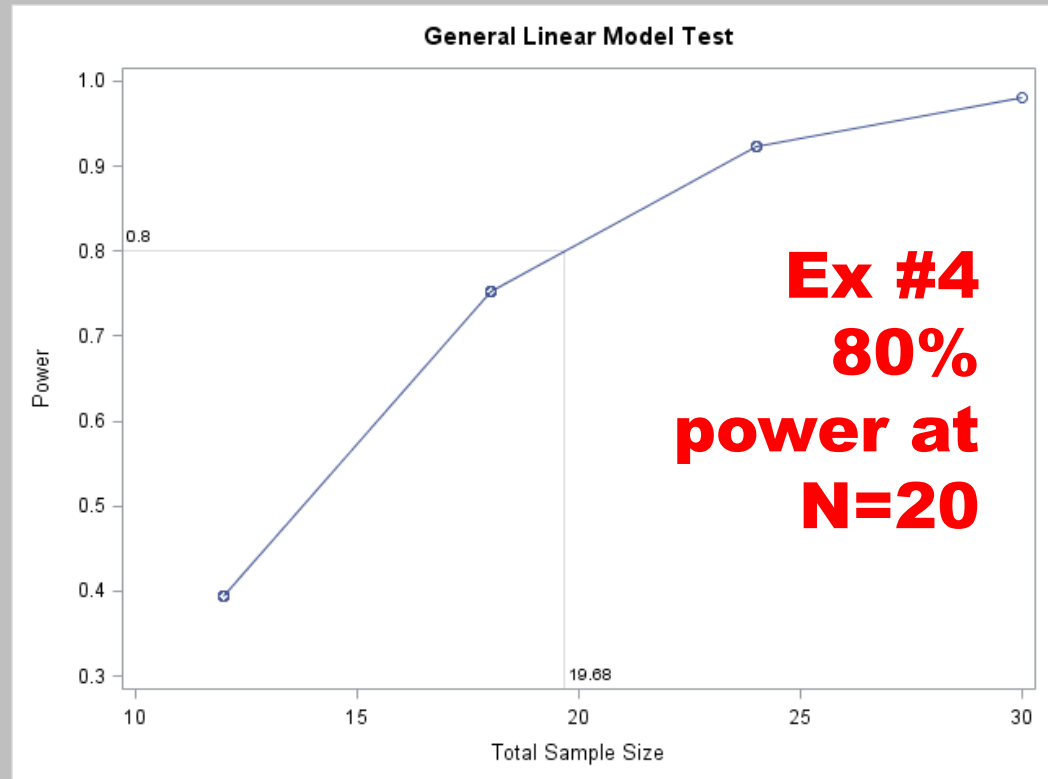
<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

Fixed Scenario Elements

| | |
|--------------------------|-----------|
| Dependent Variable | mean_set2 |
| Source | species |
| Alpha | 0.05 |
| Error Standard Deviation | 1 |
| Nominal Power | 0.8 |
| Test Degrees of Freedom | 5 |

Computed N Total

| Error DF | Actual Power | N Total |
|----------|--------------|---------|
| 18 | 0.923 | 24 |



Cuckoo Ex. 5

Stroup Ex #1

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

/* This will illustrate how to estimate the power based on the ideas of Stroup, W. W. (1999) Mixed model procedures to assess power, precision, and sample size in the design of experiments. Pages 15-24 in Proc. Biopharmaceutical Section. Am. Stat. Assoc., Baltimore, MD. The nice thing about this method is that it can be used for ANY design regardless of complexity. The idea is to

- 1. Create a data set with the structure of the design to be assessed. Instead of observed data, use the means that reflect the departure from H0 of interest.**
- 2. Run PROC MIXED with the variance and covariance components set at the anticipated values. Use the NOPROFILE and NOITER options (see below) to set the (co)variance components.**
- 3. The MODEL and CONTRAST statements in PROC MIXED compute F values which gives the non-centrality parameter.**
- 4. Pass these to a data step that estimates the power**
- 5. Plot (or print) the results. You can have several sets of means identified by the set number and separate power computations will be done for each set**

Cuckoo Ex. 5

Stroup Ex #1

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
data effect_sizes;
  set means;
  set = 1; mu = mean_set1; output;
  set = 2; mu = mean_set2; output;
  keep set species mu; ;;
```

```
proc sort data=effect_sizes;
  by set species; run;
```

```
proc tabulate data=effect_sizes;
  title2 'Effect sizes for which power computations are done';
  class set species;
  var mu;
  table set, species*mu*sum=' '*f=5.0 / rts=10; run;
```

```
/* Generate data sets for various sample sizes for later plotting purposes */
```

```
data trials;
  set effect_sizes;
  do n_per_group = 2 to 20 by 1; /* number of replicates at level of the factor */
    /* generate data with sufficient replicates all with the same mean values */
    do rep=1 to n_per_group;
      output;
    end;
  end;
  attrib n_per_group label='Number of replicates at each species';
run;
```

| set | species | | | | | |
|--------|---------|----|----|----|----|----|
| | s1 | s2 | s3 | s4 | s5 | s6 |
| | mu | mu | mu | mu | mu | mu |
| 1 hard | 21 | 22 | 22 | 22 | 22 | 23 |
| 2 Easy | 21 | 21 | 21 | 23 | 23 | 23 |

More
Code
&
Print
Trials

Cuckoo Ex. 5

Stroup Ex #1

```
proc sort data=trials;
by set n_per_group; /* group data appropriately */

proc print data=trials(obs=30);
title2 'part of the generated data'; run;
```

From loop on previous slide

| Obs | species | set | mu | N /group | rep |
|-----|---------|-----|----|----------|-----|
| 1 | s1 | 1 | 21 | 2 | 1 |
| 2 | s1 | 1 | 21 | 2 | 2 |
| 3 | s2 | 1 | 22 | 2 | 1 |
| 4 | s2 | 1 | 22 | 2 | 2 |
| 5 | s3 | 1 | 22 | 2 | 1 |
| 6 | s3 | 1 | 22 | 2 | 2 |
| 7 | s4 | 1 | 22 | 2 | 1 |
| 8 | s4 | 1 | 22 | 2 | 2 |
| 9 | s5 | 1 | 22 | 2 | 1 |
| 10 | s5 | 1 | 22 | 2 | 2 |
| 11 | s6 | 1 | 23 | 2 | 1 |
| 12 | s6 | 1 | 23 | 2 | 2 |
| 13 | s1 | 1 | 21 | 3 | 1 |
| 14 | s1 | 1 | 21 | 3 | 2 |
| 15 | s1 | 1 | 21 | 3 | 3 |
| 16 | s2 | 1 | 22 | 3 | 1 |
| 17 | s2 | 1 | 22 | 3 | 2 |
| 18 | s2 | 1 | 22 | 3 | 3 |
| 19 | s3 | 1 | 22 | 3 | 1 |
| 20 | s3 | 1 | 22 | 3 | 2 |
| 21 | s3 | 1 | 22 | 3 | 3 |
| 22 | s4 | 1 | 22 | 3 | 1 |
| 23 | s4 | 1 | 22 | 3 | 2 |
| 24 | s4 | 1 | 22 | 3 | 3 |
| 25 | s5 | 1 | 22 | 3 | 1 |
| 26 | s5 | 1 | 22 | 3 | 2 |
| 27 | s5 | 1 | 22 | 3 | 3 |
| 28 | s6 | 1 | 23 | 3 | 1 |
| 29 | s6 | 1 | 23 | 3 | 2 |
| 30 | s6 | 1 | 23 | 3 | 3 |

More
Code

Cuckoo Ex. 5

Stroup Ex #1

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
/* Show the results from ONE analysis */
```

```
proc mixed
```

```
data=trials noprofile;
```

```
/* the noprofile options prevents trying to fit the model */
```

```
title2 'Estimate the non-centrality parameter for one set of data ';
```

```
where set=1 & n_per_group=2;
```

```
by set n_per_group; Show 1 result
```

```
class species;
```

```
model mu = species; parms (&var)  
/ noiter;
```

```
/* this is where the estimated variance components are specified */
```

```
run;
```

Dimensions

| | |
|-----------------------|---|
| Covariance Parameters | 1 |
|-----------------------|---|

| | |
|--------------|---|
| Columns in X | 7 |
|--------------|---|

| | |
|--------------|---|
| Columns in Z | 0 |
|--------------|---|

| | |
|----------|----|
| Subjects | 12 |
|----------|----|

| | |
|---------------------|---|
| Max Obs Per Subject | 1 |
|---------------------|---|

Fit Statistics

| | |
|-----------------------|------|
| -2 Res Log Likelihood | 15.2 |
|-----------------------|------|

| | |
|-------------------------|------|
| AIC (smaller is better) | 15.2 |
|-------------------------|------|

| | |
|-------------------------|------|
| BIC (smaller is better) | 15.2 |
|-------------------------|------|

| | |
|--------------------------|------|
| DLIC (smaller is better) | 15.2 |
|--------------------------|------|

Type 3 Tests of Fixed Effects

| Effect | Num DF | Den DF | F Value | Pr > F |
|---------|--------|--------|---------|--------|
| species | 5 | 6 | 0.80 | 0.5876 |

Cuckoo Ex. 5

Stroup Ex #1

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
/* Estimate the non-centrality parameter  
from all the combinations */
```

```
ods select none; run;
```

```
/* turn the output off as it is not needed */
```

```
proc mixed data=trials noprofile;
```

```
/* the noprofile options prevents trying  
to fit the model */
```

```
title2 'Estimate the non-centrality  
parameter';
```

```
by set n_per_group;
```

```
class species;
```

```
model mu = species;
```

```
parms (&var) / noiter;
```

```
/* this is where the estimated variance  
components are specified */
```

```
/* save the results to the ods datasets */
```

```
ods output tests3=
```

```
whole_model_power_effects;
```

```
/* extract the F-statistic */ run;
```

```
ods select all;
```

```
run; /* turn the output back on */
```

```
proc print data=whole_model_power_effects(obs=20);
```

```
title2 'Part of the output from Proc Mixed on the fake data';
```

| Obs | set | n/ group | Effect | NumD F | DenD F | FValue | ProbF |
|-----|-----|-------------|---------|-----------|-----------|--------|-------|
| 1 | 1 | 2 | species | 5 | 6 | 0.80 | 0.587 |
| 2 | 1 | 3 | species | 5 | 12 | 1.20 | 0.366 |
| 3 | 1 | 4 | species | 5 | 18 | 1.60 | 0.210 |
| 4 | 1 | 5 | species | 5 | 24 | 2.00 | 0.115 |
| 5 | 1 | 6 | species | 5 | 30 | 2.40 | 0.060 |
| 6 | 1 | 7 | species | 5 | 36 | 2.80 | 0.030 |
| 7 | 1 | 8 | species | 5 | 42 | 3.20 | 0.015 |
| 8 | 1 | 9 | species | 5 | 48 | 3.60 | 0.007 |
| 9 | 1 | 10 | species | 5 | 54 | 4.00 | 0.003 |
| 10 | 1 | 11 | species | 5 | 60 | 4.40 | 0.001 |
| 11 | 1 | 12 | species | 5 | 66 | 4.80 | 0.000 |
| 12 | 1 | 13 | species | 5 | 72 | 5.20 | 0.000 |
| 13 | 1 | 14 | species | 5 | 78 | 5.60 | 0.000 |
| 14 | 1 | 15 | species | 5 | 84 | 6.00 | <.000 |
| 15 | 1 | 16 | species | 5 | 90 | 6.40 | <.000 |
| 16 | 1 | 17 | species | 5 | 96 | 6.80 | <.000 |
| 17 | 1 | 18 | species | 5 | 102 | 7.20 | <.000 |
| 18 | 1 | 19 | species | 5 | 108 | 7.60 | <.000 |
| 19 | 1 | 20 | species | 5 | 114 | 8.00 | <.000 |
| 20 | 2 | 2 | species | 5 | 6 | 2.40 | 0.158 |

**Show
results**

Cuckoo Ex. 5

Stroup Ex #1

<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo-power.sas>

```
/* now to compute approximations to the power */
```

```
data power;
```

```
  set whole_model_power_effects;
```

```
  nc = numdf*Fvalue;
```

```
  /* approximate non-centrality parameter */
```

```
  fcrit = finv(1-&alpha, numDF, denDF, 0);
```

```
  /* estimate critical value */
```

```
  power = 1 - probf(fcrit, numdf, dendf, nc);
```

```
  /* estimated power */
```

```
  attrib power label='Power' format=7.2;
```

```
  attrib nc label='Non-centrality' format=7.1;
```

```
  attrib fcrit label='F-critical value' format=7.2;
```

```
  drop probF;
```

```
  run;
```



**Show
results**

Cuckoo Ex. 5

Stroup Ex #1

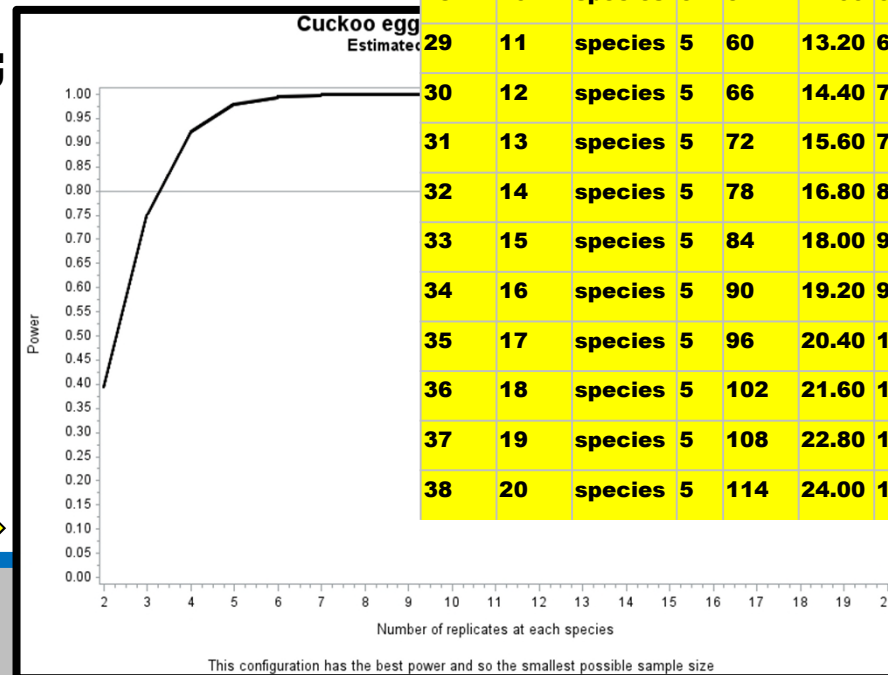
<http://people.stat.sfu.ca/~cschwarz/Stat-LinearModels/Examples/CRD.fixed/cuckoo>

```
proc print data=power label split=' ';
title2 'Estimated power using Stroup method
by set; run;
```

Show results

```
PROC GPLOT data=power;
title2 "Estimated power at alpha=&alpha";
by set;
axis1 label=(a=90 r=0
'Power') order=0 to 1 by .05;
plot power*n_per_group
/ vaxis=axis1 vref=.80;
symbol1
v=none i=join w=2 l=1; run;
ods pdf close;
run;
```

Show results



| Obs | Number of replicates at each species | Effect | Num DF | Den DF | F Value | Non-centrality | F-critical value | Power |
|-----|--------------------------------------|---------|--------|--------|---------|----------------|------------------|-------|
| 20 | 2 | species | 5 | 6 | 2.40 | 12.0 | 4.39 | 0.39 |
| 21 | 3 | species | 5 | 12 | 3.60 | 18.0 | 3.11 | 0.75 |
| 22 | 4 | species | 5 | 18 | 4.80 | 24.0 | 2.77 | 0.92 |
| 23 | 5 | species | 5 | 24 | 6.00 | 30.0 | 2.62 | 0.98 |
| 24 | 6 | species | 5 | 30 | 7.20 | 36.0 | 2.53 | 1.00 |
| 25 | 7 | species | 5 | 36 | 8.40 | 42.0 | 2.48 | 1.00 |
| 26 | 8 | species | 5 | 42 | 9.60 | 48.0 | 2.44 | 1.00 |
| 27 | 9 | species | 5 | 48 | 10.80 | 54.0 | 2.41 | 1.00 |
| 28 | 10 | species | 5 | 54 | 12.00 | 60.0 | 2.39 | 1.00 |
| 29 | 11 | species | 5 | 60 | 13.20 | 66.0 | 2.37 | 1.00 |
| 30 | 12 | species | 5 | 66 | 14.40 | 72.0 | 2.35 | 1.00 |
| 31 | 13 | species | 5 | 72 | 15.60 | 78.0 | 2.34 | 1.00 |
| 32 | 14 | species | 5 | 78 | 16.80 | 84.0 | 2.33 | 1.00 |
| 33 | 15 | species | 5 | 84 | 18.00 | 90.0 | 2.32 | 1.00 |
| 34 | 16 | species | 5 | 90 | 19.20 | 96.0 | 2.32 | 1.00 |
| 35 | 17 | species | 5 | 96 | 20.40 | 102.0 | 2.31 | 1.00 |
| 36 | 18 | species | 5 | 102 | 21.60 | 108.0 | 2.30 | 1.00 |
| 37 | 19 | species | 5 | 108 | 22.80 | 114.0 | 2.30 | 1.00 |
| 38 | 20 | species | 5 | 114 | 24.00 | 120.0 | 2.29 | 1.00 |

Proc Mixed

An Introduction to Statistical Power Calculations for Linear Models with SAS 9.1

Robin High, University of Oregon

/*Power Computations with PROC MIXED

Studies frequently utilize more complicated designs than T-tests or independent groups ANOVAs.

Researchers may compute power for studies with these simpler designs and then run the experiment with a more complex one, assuming the power results from the former act as an “upper bound” since efficiencies are produced by the chosen design. That is, if 30 subjects are deemed necessary to meet study objectives under an independent groups design (e.g., a study will have .80 power to detect a given effect), power will likely increase if a repeated measures design is chosen.

To illustrate the flexibility of PROC MIXED, its ability to compute power for the independent groups design will be shown first.

The general process is described in Chapter 12 of “SAS for Mixed Models (Littell, et. al.). With manipulation of the inputs to PROC MIXED and specifying the variance, results

from the table of “Type3 Tests of Fixed Effects” will produce the power calculation for a two-sample t-test: */

Statistical Power

Analysis Using SAS and R

Contrasts 55 pages and many examples

[http://jansenlex.readyhosting.com/pnwsug/2007/Robi
n%20High%20-
%20Statistical%20Power%20Calculations%20for%20
Linear%20Models.pdf](http://jansenlex.readyhosting.com/pnwsug/2007/Robi%20High%20-%20Statistical%20Power%20Calculations%20for%20Linear%20Models.pdf)

```
DATA anv;  
INPUT group $ mean count @@;  
* assume equal group sizes;  
CARDS;  
A 10 86 B 12 86  
;  
ODS OUTPUT tests3=tst3;  
PROC MIXED DATA=anv NOProfile;  
* add the NOProfile option;  
CLASS group;  
WEIGHT count;  
MODEL mean = group / ddf=170;  
* add the error degrees of freedom;  
PARMS (16) / NOITER ;  
* enter the assumed population variance;  
RUN;
```

```
DATA pwr;  
SET tst3; alpha = .05;  
NonCen = NumDF*Fvalue;  
Fcrit = FINV(1-alpha, numdf, dendf, 0);  
Power =  
1- PROBF(Fcrit, NumDF, DenDF, NonCen);  
run;  
  
PROC PRINT DATA=pwr NOobs;  
run;
```

Show
results

| Effect | NumDF | DenDF | FValue | ProbF | alpha | NonCen | Fcrit | Power |
|--------|-------|-------|--------|--------|-------|--------|--------|--------|
| group | 1 | 170 | 10.75 | 0.0013 | 0.05 | 10.75 | 3.8967 | 0.9032 |

Power for More Uncommon Design Situations

Simulations

Power for More Uncommon Design Situations

<http://jansenlex.readyhosting.com/pnw sug/2007/Robin%20High%20-%20Statistical%20Power%20Calculations%20for%20Linear%20Models.pdf>

```
DATA prd_t;
```

```
sigma=4;
```

```
delta=2;
```

```
crr=.25;
```

```
alpha=.05;
```

```
power=.9032;
```

```
beta=1-power;
```

```
sides=2;
```

* standard deviation of an observation = σ ;

* difference in means to be detected = Δ ;

* within subject correlation = ρ ;

* Type I error = α ;

* Power of the test = $1-\beta$;

* Type II error = β ;

* 1 or 2 sided;

* compute standard deviation of a difference of correlated values;

```
sigma_dif = sigma*SQRT(2*(1-crr));
```

```
z_a=ABS(PROBIT(alpha/sides));
```

```
z_b=ABS(PROBIT((1-beta)));
```

```
NSubj = CEIL(((z_a + z_b)**2) * ((sigma_dif/delta)**2));
```

```
RUN; PROC PRINT NOobs; run;
```

Show Results

| sigma | delta | crr | alpha | power | beta | sides | sigma_dif | z_a | z_b | NSubj |
|-------|-------|------|-------|-------|-------|-------|-----------|------|------|-------|
| 4 | 2 | 0.25 | 0.05 | 0.90 | 0.097 | 2 | 4.899 | 1.96 | 1.30 | 64 |

SIMULATION

SIMULATION

```
OPTIONS nocenter Nodate nonumber  
  linesize=MAX pagesize=MAX  
  formdlm = '-'  
  nomprint nosymbolgen nomlogic ;  
TITLE ;  
ODS GRAPHICS OFF;  
* GENERATE DATA 4 ANOVA MODEL;  
* SIMULATION SPECIFICS;  
%GLOBAL n1 n2 n3  
  mean1 mean2 mean3  
  sd1 sd2 sd3  
  ngroups nreps SeedVar;  
%LET ngroups = 3;  
%LET mean1 = 11.4;  
%LET mean2 = 16.7;  
%LET mean3 = 4.0;  
%LET sd1 = 10.0;  
%LET sd2 = 10.0;  
%LET sd3 = 10.0;  
%LET n1 = 20;  
%LET n2 = 20;  
%LET n3 = 20;  
%LET nreps = 100;  
%LET SeedVar = 7;
```

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

```
%MACRO simulateANOVA ;  
DATA ANOVAsim;  
CALL streaminit(&SeedVar.); *set random seed;  
%DO replication = 1 %TO &nreps.;  
  %DO group = 1 %TO &ngroups.;  
    %DO n = 1 %TO &&n&group.;  
      Y =  
      RAND('NORMAL',%SYSEVALF(&&mean&group.),%  
      SYSEVALF(&&sd&group.));  
      mean = &&mean&group.;  
      sd = &&sd&group.;  
      group = &group.;  
      person = &n.;  
      replication = &replication.;  
      OUTPUT;  
    %END;  
  *person loop;  
  %END; *group loop;  
%END; *replication loop;  
RUN;  
%MEND simulateANOVA;
```



**More
Code**

SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

```
%simulateANOVA;  
* Run ANOVA per dataset, save  
results;  
PROC GLM DATA =ANOVAstim;  
BY replication;  
CLASS  
group;  
MODEL y = group / SS3 ;  
ODS OUTPUT FitStatistics=R2  
ModelANOVA=SumSquares  
OverallANOVA=ANOVA  
LSMeans=Means;  
LSMEANS group;  
RUN;
```



Two Examples

SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The GLM Procedure replication=1

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|--------|----|----------------|-------------|---------|--------|
| Model | 2 | 2744.2 | 1372.1 | 15.37 | <.0001 |
| Error | 57 | 5088.6 | 89.2 | | |
| Total | 59 | 7832.9 | | | |

The GLM Procedure replication=2

```
DATA SumSquares;
SET SumSquares;
IF ProbF LT .05 THEN Signif=1;
ELSE Signif=0;
RUN;
```

More Code

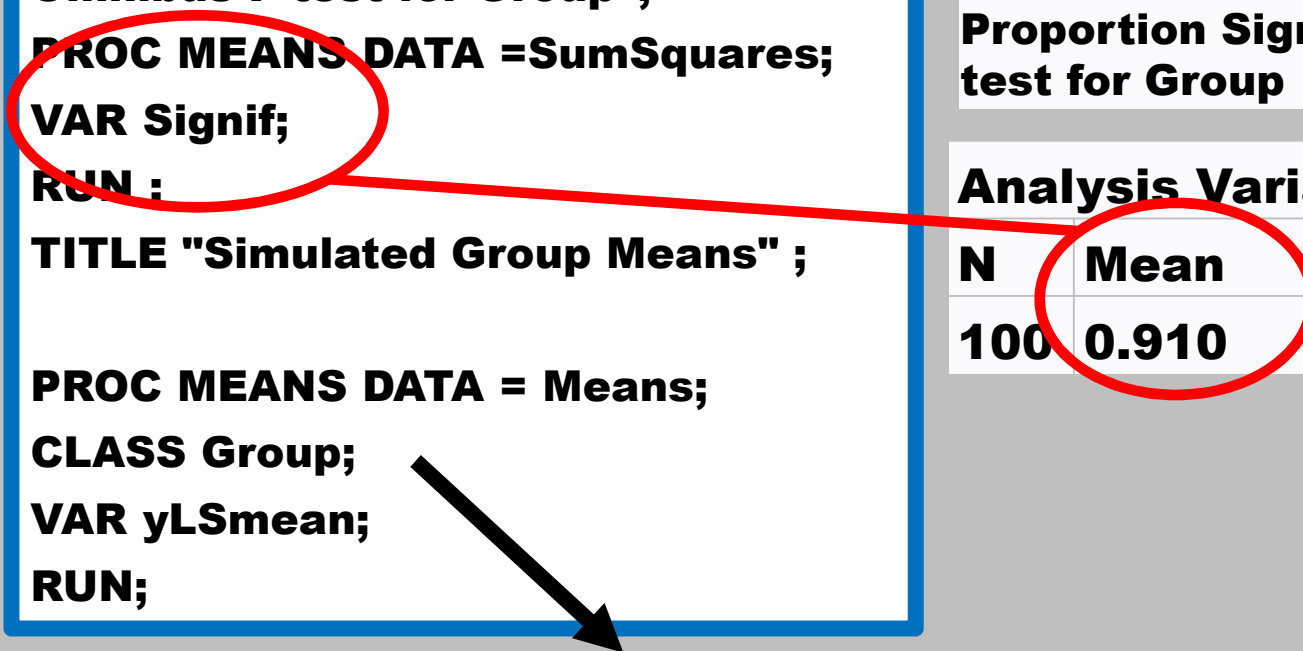
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|--------|----|----------------|-------------|---------|--------|
| Model | 2 | 669.4 | 334.7 | 2.48 | 0.0927 |
| Error | 57 | 7690.1 | 134.9 | | |
| Total | 59 | 8359.5 | | | |

| | | | |
|----------|-----------|----------|----------|
| R-Square | Coeff Var | Root MSE | Y Mean |
| 0.350348 | 92.61810 | 9.448551 | 10.20163 |

| | | | |
|----------|-----------|----------|----------|
| R-Square | Coeff Var | Root MSE | Y Mean |
| 0.080081 | 92.17956 | 11.61525 | 12.60068 |

SIMULATION

```
TITLE "Proportion Significant  
Omnibus F-test for Group";  
PROC MEANS DATA =SumSquares;  
VAR Signif;  
RUN ;  
TITLE "Simulated Group Means" ;  
  
PROC MEANS DATA = Means;  
CLASS Group;  
VAR yLSmean;  
RUN;
```



http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

Proportion Significant Omnibus F-test for Group

Analysis Variable : Signif

| N | Mean | Std Dev | Min | Max |
|------------|--------------|----------------|------------|--------------|
| 100 | 0.910 | 0.287 | 0 | 1.000 |

Analysis Variable : YLSMean Y LSMEAN

| group | N Obs | N | Mean | Std Dev | Minimum | Maximum |
|--------------|--------------|------------|--------------|----------------|----------------|----------------|
| 1 | 100 | 100 | 11.32 | 2.48 | 4.34 | 17.22 |
| 2 | 100 | 100 | 16.17 | 2.18 | 11.13 | 21.43 |
| 3 | 100 | 100 | 4.062 | 2.29 | -1.04 | 9.95 |

SIMULATION Unequal variances

```
%MACRO simulateANOVA ;  
DATA ANOVAsim;  
CALL streaminit(&SeedVar.); *set random seed;  
%DO replication = 1 %TO &nreps.;  
  %DO group = 1 %TO &ngroups.;  
    %DO n = 1 %TO &&n&group.;  
      Y      =  
RAND('NORMAL',%SYSEVALF(&&mean&group.),%SYSEVALF(&&sd&group.));  
      mean    = &&mean&group.;  
      sd      = &&sd&group.;  
      group   =&group.;  
      person  =&n.;  
      replication=&replication.;  
      OUTPUT;  
    %END;  
  *person loop;  
%END;*group loop;  
%END; *replication loop;  
RUN;  
%MEND simulateANOVA;
```

SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

*** SDs should have been 10.8, 12.4, and 7.1, but it only allows a common SD;**

```
%GLOBAL n1 n2 n3 mean1  
mean2 mean3 sd1 sd2 sd3  
ngroups nreps SeedVar;
```

```
%LET ngroups = 3;
```

```
%LET mean1 = 11.4;
```

```
%LET mean2 = 16.7;
```

```
%LET mean3 = 4.0;
```

```
%LET sd1 = 10.8;
```

```
%LET sd2 = 12.4;
```

```
%LET sd3 = 7.1;
```

```
%LET n1 = 20;
```

```
%LET n2 = 20;
```

```
%LET n3 = 20;
```

```
%LET nreps = 100;
```

```
%LET SeedVar = 77;
```

```
%simulateANOVA;
```

*** FOR UNEQUAL VARIANCES;**

```
PROC MIXED DATA =ANOVAsim
```

```
METHOD =ML;
```

```
BY replication;
```

```
CLASS group person;
```

```
MODEL y = group /
```

```
SOLUTION DDFM =KR;
```

```
LSMEANS group / PDIFF =ALL;
```

```
REPEATED / SUBJECT =person*group
```

```
GROUP =group;
```

```
ODS OUTPUT Diffs = LSMEANDIFF
```

```
Tests3 = Tests3;
```

```
RUN;
```

Two Examples

SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The Mixed Procedure replication=1

Null Model Likelihood Ratio Test

| DF | Chi-Square | Pr > ChiSq |
|----|------------|------------|
| 2 | 22.11 | <.0001 |

Fit Statistics

| | |
|-------------------|-------|
| -2 Log Likelihood | 431.7 |
| AIC (smaller 😊) | 443.7 |
| AICC (smaller 😊) | 445.3 |
| BIC (smaller 😊) | 456.3 |

The Mixed Procedure replication=2

Null Model Likelihood Ratio Test

| DF | Chi-Square | Pr > ChiSq |
|----|------------|------------|
| 2 | 3.51 | 0.1727 |

Fit Statistics

| | |
|-------------------|-------|
| -2 Log Likelihood | 443.1 |
| AIC (smaller 😊) | 455.1 |
| AICC (smaller 😊) | 456.7 |
| BIC (smaller 😊) | 467.7 |

Two Examples

SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

The Mixed Procedure replication=1

Solution for Fixed Effects

| Effect | group | Estimate | Std Error | DF | t Value | Pr > t |
|-----------|-------|----------|-----------|------|---------|---------|
| Intercept | | 2.32 | 1.27 | 20 | 1.83 | 0.0827 |
| group | 1 | 8.90 | 2.14 | 36.7 | 4.15 | 0.0002 |
| group | 2 | 13.31 | 3.73 | 25.2 | 3.57 | 0.0015 |
| group | 3 | 0 | . | . | . | . |

The Mixed Procedure replication=2

Solution for Fixed Effects

| Effect | group | Estimate | Std Error | DF | T | Pr > t |
|-----------|-------|----------|-----------|------|------|---------|
| Intercept | | 6.86 | 1.71 | 20 | 4.01 | 0.0007 |
| group | 1 | 6.54 | 3.11 | 34.5 | 2.10 | 0.0432 |
| group | 2 | 12.02 | 2.86 | 36.9 | 4.19 | 0.0002 |
| group | 3 | 0 | . | . | . | . |

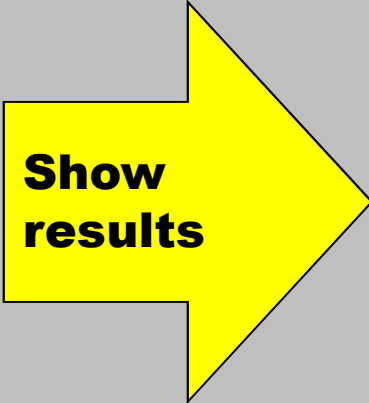
SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

```
DATA Tests3;  
SET Tests3;  
IF ProbF LT .05 THEN Signif=1;  
ELSE Signif=0;  
RUN;
```

```
DATA LSMEANDIFF;  
SET LSMEANDIFF;  
IF ProbT LT .05 THEN Signif= 1;  
ELSE Signif=0;  
RUN;
```

```
PROC SORT DATA=LSMEANDIFF;  
BY Group _Group;  
RUN;  
TITLE "Proportion Significant  
Omnibus F-test for Group";
```



**Show
results**

SIMULATION

http://jonathantemplin.com/files/multivariate/mv12psyc943/mv12psyc943_lecture21.pdf

```
PROC MEANS DATA =Tests3 MEAN;  
VAR Signif; RUN ;  
TITLE "Simulated Group Mean Differences";  
PROC MEANS DATA =LSMEANDIFF MEAN ;  
BY Group_Group;  
VAR Signif;  
RUN;  
TITLE;  
* To clear results viewer in between runs;  
ODS HTML CLOSE; ODS HTML ;
```

**Show
Results**

**Analysis Variable
: Signif**

Mean

0.9900000

Show Results

Simulated Group Mean Differences

group=1 _group=2

**Analysis Variable
: Signif**

Mean

0.3200000

group=1 _group=3

**Analysis Variable
: Signif**

Mean

0.8100000

group=2 _group=3

**Analysis Variable
: Signif**

Mean

0.9800000

The End

Russ.Lavery@verizon.net

Thanks To:

Dr. Bajgier

Russell Lavery

http://support.sas.com/documentation/cdl/en/statug/67523/HTML/default/viewer.htm#statug_glimpower_gettingstarted02.htm

Incorporating Contrasts, Unbalanced Designs, and Multiple Means Scenarios

Suppose you want to compute power for the two-way ANOVA described in the section [Simple Two-Way ANOVA](#), but you want to additionally perform the following tasks:

- try an unbalanced sample size allocation with respect to Exposure, using twice as many samples for levels 2 and 3 as for level 1
- consider an additional, less optimistic scenario for the cell means, shown in [Table 47.2](#)
- test a contrast of Exposure comparing levels 1 and 3

```
data Exemplary; input Variety $ Exposure $ HeightOrig HeightNew Weight;  
datalines; 1 1 14 15 1 1 2 16 16 2 1 3 21 20 2 2 1 10 11 1 2 2 15 14 2 2 3 16 15  
2 ;
```

```
proc glmpower data=Exemplary; class Variety Exposure; model  
HeightOrig HeightNew = Variety | Exposure; weight Weight; contrast  
'Exposure=1 vs Exposure=3' Exposure 1 0 -1; power stddev = 5 ntotal =  
60 power = .; run;
```

<https://sassyfridays.wordpress.com/2014/03/18/proc-power-and-proc-glmpower/>

a factorial design

We are now designing an ANOVA with 2×3 factorial design. We want to examine whether male and female dodo birds have different beek lengths when housed in a small, medium or large yard. We were able to obtain means and a standard deviation from a study conducted in Atlantis centuries ago and now we need to know how many dodo birds we need in order to obtain a power of 80%.

Based on the paper from Atlantis we have the following means:

Males in small yard: 12

Females in small yard: 8

Males in medium yard: 21

Females in medium yard: 21

Males in large yard: 46

Females in large yard: 39

Overall standard deviation reported in the paper was 4

```
Data atlantis;  
do sex = 1 to 2;  
do housing = 1 to 3;  
input beek_length @@;  
end;  
end;  
datalines;  
12 21 46  
8 21 39  
;  
Run;
```

To calculate sample size – we need PROC GLMPOWER

```
Proc glmpower data=atlantis;  
class sex housing;  
model beek_length = sex | housing;  
power  
stddev = 4  
ntotal = .  
power = 0.80;
```

```
Run;
```